Abstract

We consider a multi-community city where community quality is linked to residents’ civic efforts like being proactive in preventing crime and in ensuring the quality of publicly provided goods. Homeownership increases incentives for such efforts, but credit market imperfections force the poor to rent. Within-community externalities can lead to segregated cities – with the rich living with rich in healthy homeowner communities, and the poor living with poor in dysfunctional renter communities. The pattern of tenure segregation across communities in the US accords well with our prediction. We study alternative tax-subsidy policies to alleviate inefficiencies in the housing market, and identify the winners and losers under such policies.
“New Yorkers who lived through the arson and looting that ravaged the city during the blackout of 1977 were understandably edgy when the lights went out on August 14 [2003]. But it was clear by late evening that … [1]his night did not belong to arsonists or looters. … An important difference between this blackout and the last one is the massive, publicly financed reconstruction effort that has rebuilt neighborhoods like the South Bronx from scratch. The program, begun by Mayor Edward Koch in the 80's, has produced more than 200,000 affordable apartments and houses, revitalizing burned-out communities and turning record numbers of New Yorkers into homeowners with a vested interest in keeping their areas safe.”

_New York Times_ editorial, 8/24/2003

The nature of communities has become a central concern in every society. A large empirical literature shows that homeownership makes a difference for civic quality (see the references below). In the US, many cities are segregated between homeowner communities and renter communities (see the evidence in Section 1.2); there is a high correlation between the latter and violent crime-ridden neighborhoods (see Sampson et al. 1997); and growing up in such neighborhoods has a profound negative impact on health, personal development, and school outcomes (see Leventhal and Brooks-Gunn 2000).

The existing theoretical literature on homeownership does not adequately explain these phenomena. Some authors do not model the dependence of housing tenure choice on community characteristics, treating the latter as fixed (e.g., Henderson and Ioannides 1983). Others suggest that crime in renter communities is a simple consequence of poverty: “it is the poverty associated with poor housing, rather than the housing _per se_, that causes these costly social problems” (Rosen 1985, p.378).

This paper presents a model that challenges these views. We show that households with identical preferences and similar abilities to create healthy neighborhoods may nonetheless _self-organize_ into communities with starkly different characteristics. An interplay of within-community externalities and market forces can lead to cities that are segregated by tenure and income – with the rich living with rich in homeowner communities with well-functioning civic environments, and the poor living with poor in dysfunctional renter communities. The predicted segregation between homeowners and renters accords well with the actual housing tenure segregation in the US, which we document for the first time.

Our model provides a theoretical framework to evaluate alternative housing policies. The centerpiece of US urban development policy is to expand homeownership among low-income households (Department of Housing and Urban Development, 1991). It has been claimed that “a critical mass of homeowners can turn around the dynamic of a distressed neighborhood” (Washington Post,
4/12/97), and that “if there is a silver bullet in urban redevelopment, it is homeownership” (New York Times, 4/16/98). Recent policy initiatives have also focused on the social benefits of promoting co-residence of homeowners and renters in a community. The Moving to Opportunity demonstration, which has been operating in five US cities since 1994, involves moving families from the least desirable housing projects to safer home-owning neighborhoods (see Katz et al., 2001). We use our model to analyze both kinds of policies – housing subsidy schemes to raise homeownership rates, and policies to encourage homeowners and renters to live together.

Our premise is that a community’s civic environment – its local institutions, the crime situation, etc. – greatly influences the well-being of residents. Residents can expend effort to enhance the civic quality of their homes and their community – improve security by being vigilant against crime; ensure quality supply of publicly provided goods by participating in the running of local institutions, voting in local elections, and demonstrating against government inaction, etc. Such civic efforts share the following features: individual effort generates positive spillovers for community neighbors, there are complementarities in the costs and benefits to such effort, and sustained civic efforts lead to durable improvements in the community environment and increases in property values (see Section 1.1 for evidence).¹

However, individual effort is not contractible. A household chooses its effort level in its self-interest, given its perceived private returns from such effort. That is why ownership matters. While all residents gain to the same extent from an improvement in civic quality, homeowners also gain from the increase in their property value. As a result, homeowners are more likely to expend greater civic effort. But then why don’t all community residents become homeowners? Because, given imperfections in the credit market, the cost of borrowing to purchase a home is substantially higher for the poorer residents.²

In a city with many communities, we study the implications of these features on the effort, tenure, and location decisions of households with different incomes, and on the community outcomes that these

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¹ Another important feature of most civic actions is that one has to be a community resident to take effective actions. ‘Absentee landlords’ will have much higher costs than residents of obtaining information about shocks to the home and the community, and of responding to such shocks. Further, they will not have the same incentives to take such actions since they are not directly affected by community quality but only by its effect on property values.
² Down-payment and debt service provisions prevent a majority of renters in the US from becoming homeowners. Savage (1999) reports that in 1995, 70% of families that rented in the US were unable to purchase a $20,000 home.
decisions generate. Formally, we construct a ‘multi-community social interactions model’ that links community characteristics with individual actions.\(^3\) We embed in it an agency problem that arises from the non-contractibility of effort. The co-existence of local interaction effects and a moral hazard problem has the following consequences for community formation and individual welfare.

First, there is a ‘wealth effect on incentives’: within a community, homeowners are richer than renters and, since ownership contracts provide better incentives, expend greater civic effort.\(^4\) Second, individual tenure decisions depend on the community tenure distribution since that influences the returns to investing in a home. As a result, there exists a within-community ‘social multiplier’: when some households switch from renting to owning, that by itself induces their neighbors to make similar switches. This can lead to a coordination problem and generate multiple equilibria.

Third, if homeowners are willing to pay even slightly more than renters for an improvement in community quality (which will be the case under plausible conditions), they will ‘agglomerate’ by out-bidding renters. This will lead to tenure segregation, with homeowner communities having a better civic environment and higher property values than renter communities. Finally, it may be the case that if one household is richer than another, the former is willing to pay more for an improvement in community quality than the latter. Then there will be segregation both by tenure and by income, and all residents of a ‘better’ community will be richer than all residents of a ‘worse’ one.\(^5\)

We thus provide an explanation of the co-existence ‘good’ and ‘bad’ communities that does not rely upon differences among individuals in preferences or abilities, but upon differences among collectivities that arise endogenously due to positive feedback effects of non-contractible effort.

\(^3\) Schelling (1971), de Bartolome (1990), Bénabou (1993, 1996), and Durlauf (1996) are seminal papers in the social interactions literature; also see the surveys by Fernandez (2001) and Durlauf (2003).

\(^4\) In this, our paper relates to agency models exhibiting wealth effects on incentives by Galor and Zeira (1993), Legros and Newman (1996), and Mookherjee and Ray (2002) among others.

\(^5\) In our ‘behavioral peer groups’ model, an agent’s utility is affected by the behavior of his neighbors (i.e., their effort choice) and not by their types (i.e., rich or poor). As a result, the forces that lead to segregation with respect to endogenous behavior (tenure segregation) are not identical to those that lead to segregation with respect to exogenous types (income segregation). In Section 4.2, we show the connections between these two dimensions of segregation.

Bénabou (1993) and Brock and Durlauf (2001) also model behavioral peer groups. In the former paper, agents behave differently in equilibrium because the technology exhibits diminishing returns to behaving in the same way as others. In the latter paper, exogenous preference differences cause behavior heterogeneity. Helsley and Strange (2000) consider a model where heterogeneous residents choose different actions with local externalities; the authors study the secession of a group of residents from a single community, and not free-mobility equilibria in a multi-community city.
An important consequence of this is that community equilibria need not be constrained Pareto efficient. Specifically, there may be ‘too few’ homeowners in a city because of uncompensated externalities from homeownership. This problem can be compounded by a coordination failure in tenure choice. In addition, equilibrium tenure segregation may be inefficient: the agglomeration of homeowners and renters in distinct communities can adversely affect average community quality.

We study alternative tax-subsidy policies that address each kind of inefficiency. We show that housing subsidy policies can enhance efficiency by improving the city’s ‘tenure profile,’ and can do so more cost-effectively when subsidies can be appropriately ‘targeted.’ We then present a novel tax-subsidy scheme that can induce a ‘stable integration’ of homeowners and renters.

An important feature of such policies is that they are likely to generate both ‘winners’ and ‘losers.’ While middle class homeowners benefit from a housing subsidy scheme (especially those who become homeowners under the scheme), low-income renters can be hurt as the scheme is likely to raise their rents. The identities of winners and losers will be very different under a policy that integrates communities by tenure – co-residence with homeowners can make all renters better off while all homeowners can be worse off as property values fall. This helps understand the opposition that desegregation schemes have generally met. For instance, in a protracted legal conflict over the right of a non-profit organization to build low-income housing in a New Jersey community, the community would accept low-income residents if they were homeowners, but not if they were renters (Newsday 3/7/96).

We proceed as follows. Section 1 presents the empirical evidence that motivates our study. We set up the model in Section 2, and solve for individual tenure choices in Section 3. Community equilibria are characterized in Section 4. In Section 5, we discuss the nature of inefficiencies in such equilibria and study corrective policies. Section 6 contains our concluding remarks. Appendix I discusses a general agency model of tenure contracting; proofs are presented in Appendix II; and Appendix III contains an example of equilibria in a two-community city.

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6 This complements and extends the policy analysis of Fernandez and Rogerson (1996), who study a model where households with different incomes have different preferences over locally-financed education. Their study is carried out in a simpler framework where there is no housing market, and thus there are no ‘price effects’ of relocating a household from one community to another.
1. Empirical Evidence

1.1 Community Interactions and Incentive Effect of Homeownership

In this section, we report the findings of existing empirical studies that document community interaction effects, and those that demonstrate that homeowners are ‘better citizens’ than renters.

In a study of Chicago neighborhoods, Sampson et al. (1997) find that the most important influence on a community’s crime rate is the residents’ willingness to respond to threats to community safety. Besley and Burgess (2002) and Stromberg (2004) show that state and local governments are more responsive in areas where information flows are more developed and political participation is greater.

These studies indicate that individual actions generate within-community spillovers. While a household is primarily motivated by self-interest to take such actions, e.g., improve the safety of its home, ensure adequate access to publicly provided goods, etc., its effort creates an ‘impure local public good’ – a good that provides utility to the household and raises the market value of its home, and also provides similar benefits to its community neighbors, albeit to a lesser degree.

Cohen and Dawson (1993) find that living in extremely poor communities, where the civic participation of the poor is low due to their limited education and income, leads the non-poor to politically disengage as well. This indicates the existence of complementarities between individual and group actions. Specifically, when the aim is to improve the functioning of local institutions and/or to deter crime, there is obvious ‘strength in numbers.’ An attempt to bring criminals to justice can be very costly for an individual if he is working alone. In a study of the central district of a major Northeastern US city, Merry (1981, p.142) estimates that 40% of burglaries of black families are retaliatory acts against households that are perceived to have ‘big mouths’ (i.e., those who report crimes to the police).

A number of studies show that the benefits of civic actions persist over time and raise property values. Pargal and Wheeler (1996) find that pressure from community residents is very effective in long-term reduction in pollution from industrial plants, and Smith and Huang (1995) show that reductions in air pollution are capitalized into housing prices. Buck et al. (1991) establish that decreases in crime are strongly positively related to housing prices.

There is also substantial empirical evidence that controlling for observables, homeowners expend
greater civic effort than renters. Table 1 summarizes some recent studies that find that homeowners are significantly more likely to be engaged in neighborhood activism when facing a threat to its home and community (Cox 1982), to be involved in community organizations (Rohe and Stegman 1994), and to vote in local elections (Verba et al. 1995, DiPasquale and Glaeser 1999).

The joint hypothesis of the incentive effect of homeownership and durable improvements in home and community quality resulting from residents’ civic efforts predicts that property values should be rising in the number of homeowners in a community. Controlling for the composition of a community by race and education, Coulson et al. (2001, p.5) find that “higher rates of ownership in neighborhoods are indeed accompanied by higher housing prices within the neighborhood.”

1.2 Tenure Segregation
We now present primary evidence that homeowners desire to co-reside with other homeowners. We utilize the 1990 US Census data to empirically study the pattern of tenure segregation across communities in the US. We use data on the ten largest metropolitan areas (MSAs), covering 37% of the population. We proxy for ‘communities’ with census tracts, which are areas of between 2,500 and 8,000 people separated by boundaries such as rivers, highways, or major streets.\footnote{The data show that poorer families are more likely to rent; the fraction of families with children who are homeowners rises from 31\% to 65\% as annual income rises from the $15,000-25,000 to the $35,000-50,000 bracket.}

We report the commonly used index of spatial segregation – the ‘dissimilarity index,’ analyzed in Massey and Denton (1988). In our context, the index answers the question: Within an MSA, what fraction of the population needs be relocated so that each tract has the same proportion of homeowners and renters as that of the MSA? The index ranges from zero (when all tracts have the same ratio of owners to renters) to one (when owners and renters do not co-reside in any tract). Since there is evidence that race and income cause segregation (Schelling 1971, Cutler et al. 1999), we calculate the index separately for families with different attributes. The index for households with attribute $\chi$ is:

$$
\text{Dissimilarity index} = \frac{\sum_i \left| \frac{rh_{i\chi}}{RH_{\chi}} - \frac{oh_{i\chi}}{OH_{\chi}} \right|}{2},
$$
where, for families with attribute \( \chi \), \( rh_\chi \) (resp., \( oh_\chi \)) is the number of renter (resp., owner) households in the tract, and \( RH_\chi \) (resp., \( OH_\chi \)) is the total number of renter (resp., owner) households in the MSA.

Table 2 shows that the dissimilarity index is moderate to high for every income class and race. In each income bracket, approximately 60% to 80% of black households would have to move for each tract to have the same owner/renter composition as that of the MSA. The corresponding number for non-black families with children ranges from 40% to 60%.\(^8\) This pattern of tenure segregation cannot be explained by race or income or the presence of children, because it occurs within household groups with similar attributes. Our analysis provides an explanation for this phenomenon.

2. The Model

Consider a city consisting of \( N (>1) \) communities, each having single-family homes of measure \( 1/N \). The housing units are physically identical, and are owned by a large number of infinitely-lived risk-neutral real estate companies. A generation of households moves into the city at the beginning of every period, and moves out at the end of the period (when the next generation moves in).\(^9\) For simplicity, we take the number of households in every generation to be the same as the total number of homes in the city: a continuum of measure one. In each generation, households are identical in all respects except their current (endowed) income \( y \), which is distributed across households according to \( F(.) \) on an interval \([y^-, y^+]\). Each household’s (common) future income is \( w \).

Our model is essentially static in that we focus on the behavior of a particular generation of households. After a household has received its income \( y \), it selects a home in one of the \( N \) communities and negotiates a ‘tenure contract’ with the relevant real estate company. This contract is a pair \( \{\alpha, \beta\} \): for an up-front payment \( \beta \), the household acquires the right of residence for the period and the right to a fraction \( \alpha \) of the price of the home at the end of the period. The fraction \( \alpha \) is a household’s home equity

\(^8\) The extent of tenure segregation is comparable to that of racial segregation. Cutler et al. (1999) find that for blacks and whites in all US cities in 1990, the dissimilarity index was 0.56. We find that the pattern of tenure segregation is similar across the ten MSAs, but Table 2 reports only a weighted average (with weights based on MSA population).

\(^9\) We think of a generation as composed of families who enter the city when the family is formed, reside there during the working lives of the adults, and move away when they retire. Our assumption that real estate companies own the homes simplifies the analysis without being crucial to it; see Bénabou (1996) for a similar assumption.
We will refer to a contract with a sufficiently large \( \alpha \) (defined in (2)) as an ‘ownership contract’.\(^{10}\) A contract with \( \alpha = 0 \) is a ‘rental contract’; we let \( \rho \) denote the rent (i.e., \( \beta = \rho \) for \( \alpha = 0 \)).

2.1 Community Quality

A household’s utility from living in a home derives from the ‘civic quality’ of the home – its security, the quality of publicly provided community goods, etc. – which, in turn, depends on the resident’s own civic effort and on the efforts of his community neighbors. We assume that the initial civic quality is the same for all homes in the city, and set its value at zero. We then study how differences in household effort lead to heterogeneity in civic quality across communities.

After signing a tenure contract, each household decides on its level of civic effort. While there are many dimensions to such effort, for brevity we assume that there are two actions, \( a \in \{e, n\} \), where \( e \) is high effort and \( n \) is negligible effort. The ‘current’ civic quality of a home is \( q(a, x) \), where \( x \) is the fraction of community residents who expend high effort. We refer to \( x \) as the community effort level; this is what distinguishes one community from another. While a home’s civic quality obviously rises in resident effort, i.e., \( q(e, x) > q(n, x) \), we assume that it increases in community effort \( x \) – a ‘spillover effect,’ and that a household’s marginal return to effort also increases in \( x \) – a ‘complementarity effect.’

**Assumption 1 (Community Interaction Effects):** (i) \( q_x(a, x) > 0 \), and (ii) \( q_x(e, x) > q_x(n, x) \).\(^{11}\)

The evolution of housing prices depends on the evolution of home quality. We take the ‘future’ civic quality of a home (i.e., its quality at the beginning of the following period) to be \( \gamma q(a, x) \), where \( \gamma \in (0, 1) \) is the one-period depreciation factor; thus, a part of the current quality persists in the future. To keep things simple, we take as primitive the ‘future price function’ \( P(\gamma q) \), with \( P'(\cdot) > 0 \). We let \( p(a, x) \equiv P(\gamma q(a, x)) \), and assume that \( P(\cdot) \) is not too concave so that \( a \) and \( x \) affect the future price of a home in

\(^{10}\) This is similar to the limited equity housing contracts studied in Simon (1991). Most actual tenure contracts are simpler, offering either 0 or 100% ownership (\( \alpha = 0 \) or \( \alpha = 1 \)). Our results remain valid under such 0–1 contracts.

\(^{11}\) If there were a finite number of households \( \{1, \ldots, m, \ldots, M\} \) living in \( M \) homes, we would specify that the quality of home \( m \) is \( q(a_m, \sum_{m' \neq m} a_{m'}) \), with \( q_1 > q_2 > 0 \), and \( q_{12} > 0 \). When there is a continuum of households, each household is atomistic in its contribution to community effort, and we cannot distinguish between aggregate community effort \( \sum_{m \neq m'} a_m + \sum_{m' \neq m} a_{m'} \) and the effort of neighbors from household \( m \)’s point of view \( \sum_{m' \neq m} a_{m'} \). Given that, our specification that \( q \) depends on both \( a \) and \( x \) is intended to capture the idea that individual effort produces an impure local public good.
the same way that they affect its current quality: \( p(e, x) > p(n, x) \), and \( p_s(e, x) > p_s(n, x) > 0 \).

2.2 The Incentive Problem

We posit that households desire consumption smoothing. We capture this in a simple way by assuming a minimum subsistence level for the consumption good, below which a household’s utility is unboundedly low. For simplicity, the subsistence level is set at zero. A household chooses its equity share (\( \alpha \)), effort level (\( a \)), and borrowing (\( b \)) to maximize its lifetime utility:

\[
\begin{align*}
  u &= \begin{cases} 
    [y - \beta + b] + [q(a, x) - a] + \delta[w - (1+r_B)b + \alpha p(a, x)] & \text{if } y - \beta + b \geq 0, \\
    -\infty & \text{otherwise}
  \end{cases} 
\end{align*}
\]

(1)

where \( \delta \) is the (common) discount factor, \( r_B \) is the borrowing rate, and the utility cost of effort \( a \) is \( a \).\(^{12}\)

First-period utility depends on net current income \([ y - \beta + b ]\) and home civic quality less the disutility of effort \([ q(a, x) - a ]\), and second-period utility depends on net future income \([ w - (1+r_B)b + \alpha p(a, x) ]\).

ASSUMPTION 2 (Credit Market Imperfection): The gross borrowing rate \((1+r_B)\) exceeds the marginal rate of time preference \((1/\delta)\), which in turn is no less than the gross savings rate.

This simple specification of a credit market imperfection implies the existence of a positive ‘borrowing wedge’ \( c \equiv [\delta(1+r_B) - 1] \). This wedge discourages borrowing when \( \beta \leq y \); but when \( \beta > y \), a household has to borrow \((\beta - y)\) for subsistence. No household has a strict preference to save.

Given community effort level \( x \), denote the current surplus to a household from expending high effort (relative to low effort) by \( s_0(x) \equiv [q(e, x) - e] - [q(n, x) - n] \), and the future capital gains by \( s_1(x) \equiv p(e, x) - p(n, x) \). If the household’s equity share is \( \alpha \), its net payoff from high effort is \( \{ s_0(x) + \alpha \delta s_1(x) \} \).

ASSUMPTION 3 (Incentive Problem): For all \( x \in [0, 1] \), \( \{ s_0(x) + \alpha \delta s_1(x) \} \) increases in \( \alpha \) and is strictly negative for \( \alpha = 0 \) and strictly positive for \( \alpha = 1 \).

Assumption 3 implies that there exists a critical equity share \( \alpha^* \in (0, 1) \), defined by:

\(^{12}\) In specifying (1), we assume that not being a resident in the city leads to a large negative utility for a household so that it does not consider that option. We also assume that when a household finds it optimal to borrow, it is able to repay its debt. Introducing default possibilities will not affect our result that a household will own if and only if its income is above a threshold level (see Proposition 1). This result will also hold when a household’s future income \( w \) depends on its current income \( y \) (as opposed to being constant) as long as lifetime income \([ y + \delta w(y) ]\) is increasing in \( y \).
such that a household will expend high effort if and only if its home equity share is no less than $\alpha^*$. In the next section, we determine a household’s optimal tenure choice. We show that the incentive problem leads to a situation where the rich buy enough home equity so as to have the incentive to expend high effort, while the poor do not. This moral hazard problem arises due to the non-contractibility of effort (which is assumed to be unobservable to real estate companies), the households’ desire to smooth consumption, and the borrowing wedge. In Appendix I, we present a more general agency model of tenure contracting and demonstrate the robustness of this result.

3. Tenure Choice

Consider a household residing in a community where the rental rate is $\rho$ and the community effort level is $x$. As the household is atomistic, it takes $\{x, \rho\}$ as given. We model contract negotiation between the household and a real estate company as follows: The household selects its home under the ‘default’ rental contract $\{0, \rho\}$. It can then renegotiate to a positive-equity contract $\{\alpha > 0, \beta > \rho\}$. The price $\beta$ of equity share $\alpha$ is determined by a take-it-or-leave-it offer by the household to the real estate company, with the status quo point of no renegotiation.

Under the rental contract $\{0, \rho\}$, a household expends negligible effort and receives utility:

$$u^\prime(y, x, \rho) = [y - \rho] + [q(n, x) - n] + \delta w,$$  \hspace{1cm} (3)

and the present value of the home is $[\rho + \delta p(n, x)]$. If the household renegotiates to buy equity share $\alpha$, it has to pay a price $\beta(\alpha| x, \rho)$ that is defined by: $\rho + \delta p(n, x) = \beta(\alpha| x, \rho) + \delta(1 - \alpha)p(a^0(\alpha, x), x)$. The RHS is the present value payoff to the real estate company under $\{\alpha, \beta\}$ given the household’s ‘sequentially optimal’ effort $a^0(\alpha, x)$ which equals $e$ (resp., $n$) if $\alpha \geq$ (resp. $\alpha <$) $\alpha^*(x)$.

Let $\beta^*(x, \rho) \equiv \beta(\alpha = \alpha^*(x)| x, \rho)$ denote the price of the critical equity share $\alpha^*(x)$. Then:

$$\beta^*(x, \rho) = \rho + \alpha^*(x)\delta p(n, x) - S(x),$$  \hspace{1cm} (4)

where $S(x) \equiv s_0(x) + \delta s_1(x)$ is the ‘total surplus’ from high effort. The logic behind (4) is as follows: For
a household expending negligible effort, a real estate company will charge \([\rho + \alpha*\delta p(n,x)]\) for equity share \(\alpha*\). But once a household buys \(\alpha*\) both parties realize that it will put in high effort, and that leads to the discount \(S(x) = s_0(x) + \alpha*\delta s_1(x) + [1-\alpha*]\delta s_1(x)\), where \(s_0(x)\) is the current cost of high effort and \(\alpha*\delta s_1(x)\) is the minimal incentive payment required to elicit that effort. The remaining surplus \([1-\alpha*]\delta s_1(x)\) goes to the household as it has all the bargaining power in renegotiation.\(^{13}\)

We refer to \(\beta*(x, \rho)\) as the ‘price of homeownership’: if a household invests this amount in home equity, it obtains a large enough share of the capital gains to have the incentive to expend high effort.\(^{14}\) We will call a household that invests at least \(\beta*\) in home equity a ‘homeowner,’ and one that does not a ‘renter.’ Figure 1 depicts the set of available contracts \(\{\alpha, \beta\}\) in community \(\{x, \rho\}\).

Lifetime utility under the contract \(\{\alpha*, \beta*\}\) is: \(u''(y, x, \rho) + S(x) - \max\{c[\beta*(x, \rho) - y], 0\}\). Thus, every household with income below \(\beta*(x, \rho)\) faces a trade-off: a share of home equity sufficient to provide incentive for high effort enables it to obtain the surplus \(S(x)\), but imposes a cost \(c(\beta* - y)\). Equating the two defines an ‘income threshold’ for home-buying:

\[
y^*(x, \rho) = \beta*(x, \rho) - S(x)/c. \tag{5}\]

**Proposition 1.** A household \(y\) in community \(\{x, \rho\}\) rents and expends low effort if \(y < y^*(x, \rho)\), while it becomes a homeowner and expends high effort if \(y > y^*(x, \rho)\). The household’s indirect utility is:

\[
V(y, x, \rho) = \begin{cases} 
  u''(y, x, \rho) & \forall y \leq y^*(x, \rho) \\
  u''(y, x, \rho) + S(x) - c[\beta*(x, \rho) - y] & \forall y^*(x, \rho) < y < \beta*(x, \rho) \\
  u''(y, x, \rho) + S(x) & \forall y \geq \beta*(x, \rho)
\end{cases} \tag{6}
\]

This result demonstrates the effect of wealth on incentives. The rich can afford to buy ownership

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13 This surplus allocation results from our assumption that households can make take-it-or-leave-it contract offers; any other contract negotiation process that gives households some of the surplus will yield similar results. We maintain the plausible assumptions that \(y > \rho\) for all \(y\) (so that no one has to borrow to pay rent) and that \(\beta*(x, \rho) > \rho\) for all \(x\).

14 A homeowner may have an additional incentive to expend more effort than a renter because he expects to live in the community for a longer time. While there is some evidence for this, Verba et al. (1995, Table 15.12) and DiPasquale and Glaeser (1999) find that mobility explains only a part of the difference between the behavior of owners and renters. Green and White (1997) and Sampson et al. (1997) find that ownership has effects on outcomes for children and for community quality that cannot be accounted for by mobility. We have intentionally taken mobility to be identical for all households, while recognizing that the ‘mobility argument’ complements our own.
contracts while the poor are stuck with rental contracts. As the former contracts impart greater residual claim, the rich homeowners ‘solve’ the incentive problem and expend greater civic effort than renters.

However, that is only a part of our story. The magnitude of a household’s incentive problem depends not only on its income, but also on community characteristics \( \{x, \rho\} \). By the complementarity effect, \( \alpha^* \) is a decreasing function of \( x \). Further, when that effect is strong relative to the spillover effect, the income threshold \( y^* \) is also a decreasing function of \( x \). Then the following condition holds:

**Decreasing Threshold Condition (DT):** \( y^*_x(x, \rho) < 0 \ \forall x \).

Under DT, all residents in a community are better off with an increase in \( x \) (for a fixed \( \rho \)), and homeowners gain more than renters: \( V_x^*(y^*_x) > V_x^*(y^*_r) > 0 \). Next, consider the marginal rate of substitution between community effort and rent \( (MRS_{x, \rho}) \) for the three types of households: renters, ‘mortgagees’ (i.e., homeowners that borrow), and self-financed owners. From (5) and (6), we have:

For renters:
\[
\frac{dp}{dx} \bigg|_{y^*_x} = q_x(n, x) \tag{7a}
\]

For mortgagees:
\[
\frac{dp}{dx} \bigg|_{y^*_x < y^*_r} = \frac{q_x(n, x) - cy_x^*(x, \rho)}{1 + c} \tag{7b}
\]

For self-financed owners:
\[
\frac{dp}{dx} \bigg|_{y^*_x} = q_x(n, x) + S'(x) \tag{7c}
\]

All homeowners, because they obtain the surplus \( S(x) \), ‘take out’ more from a community than renters. But mortgagees have a higher marginal cost of funds than the others. So, while \( MRS_{x, \rho} \) is always greater for self-financed owners than renters ((7c) > (7a)), that is not necessarily the case between mortgagees and renters. To have (7b) > (7a) we need the following condition:

**Single Crossing in Tenure (SCT):** \( -y^*_x(x, \rho) > q_x(n, x) \ \forall x \).

The SCT condition (which subsumes DT) holds when the complementarity effect is sufficiently

\[\frac{d\alpha^*}{dx} = -\alpha^*(x) \left\{ \left[ (s_0'(x)/s_0(x)) - (s_1'(x)/s_1(x)) \right] + \alpha^*(x) \right\}, \]

which is strictly negative since \( s_0(.) \) and \( s_1(.) \) are strictly increasing in \( x \) by Assumption 1(ii). From (5), \( y^*_x(x, \rho) = \delta_p(n, x)(d\alpha^*/dx) - (1+c)S'(x) + \alpha^*(x)\delta_p(n, x), \) where the first two terms are negative by the complementarity effect, and the last term is positive by the spillover effect.
stronger than the spillover effect. Then the indifference curves of owners and renters satisfy ‘single crossing’: homeowners have a higher marginal willingness-to-pay for community effort than renters. But \( SCT \) does not guarantee that a richer household is always willing to pay more for an increase in \( x \). For such ‘global’ single crossing, we need the following condition to ensure that \((7c) > (7b) > (7a)\):

\[
Single Crossing in Income (SCI): \quad \frac{1+c}{c} S'(x) + q_x(n, x) > -y_x*(x, \rho) > q_x(n, x) \quad \forall \ x.
\]

While the second inequality in \( SCI \) is simply \( SCT \), the first inequality requires that the complementarity effect not be too large. Mortgagees can benefit in two ways from an increase in \( x \): it increases the return to high effort, and it can reduce the price of homeownership \( \beta^* \) and thus the amount to be borrowed. If the latter effect is large, mortgagees may be willing to pay more for an increase in \( x \) than self-financed owners. \( SCI \) rules that out by bounding the complementarity effect.

In the next section, we study the implications of \( DT \), \( SCT \), and \( SCI \), which are successively more stringent conditions, on the structure of equilibria in a multi-community city.

4. Equilibrium

To specify a multi-community equilibrium, we fix the rental rate in any one community at some \( \rho_1 \), and express the equilibrium rental rates in all other communities in terms of \( \rho_1 \). In equilibrium, the rent will be the same for all homes within a community since they all have the same initial civic quality and are identically affected by local interactions. An \( N \)-community equilibrium is defined as follows.

For community \( i \), let \( \rho_i \) be the rental rate, \( x_i \) the fraction of homeowners, and \( Y_i \) the set of residents (where a household is identified by its current income). Pegging the rent in community \( k \) at \( \rho_1 \), an \( N \)-community equilibrium is a vector \( \{ \rho_i^*, x_i^*, Y_i^* \}_i \) such that (1) households are equally divided across

\[^{16}\text{SCT is equivalent to: } [\delta p(n, x)(-d \alpha^*/dx) + (1+c/s) S'(x)] > [q_x(n, x) + \alpha^*(x) \delta p_x(n, x)], \text{where the LHS is positive by the complementarity effect and the RHS is positive by the spillover effect. Note that the LHS may be larger in reality than it is in our model with a fixed borrowing wedge } c. \text{ In assessing the collateral of a home loan, appraisers take into account the proportion of owner-occupied homes in the neighborhood (Reynolds 1983, p.133). Banks perceive that a smaller fraction of such homes increase default risk, and thus charge higher interest rates. A higher } x \text{ in a community then increases the return to homeownership for an additional reason – the borrowing wedge falls (c'(x) < 0).}]

\[^{17}\text{In this, our approach is similar to that in de Bartolome (1990) and Bénabou (1996). The need to fix } \rho \text{ in one} \]
the communities, (2) no household wants to relocate: $V(y, x_i^*, \rho_i^*) \geq V(y, x_j^*, \rho_j^*)$ for all $y \in Y_i^*$, for all $i$ and for all $j \neq i$, and (3) there is ‘within-community equilibrium’ in every community.

A within-community equilibrium is described by the fraction of homeowners in the community, or equivalently, by the community effort level. Consider any community $i$ with its set of residents $Y_i$. Let $F_i$ be the truncation of the income distribution function $F$ on $Y_i$. Given $\rho_i$ and $F_i$, community effort $x_i$ maps to a unique income threshold $y^*(x_i, \rho_i)$ and thus to a set of residents who want to own. Then $x_i^*$ is a within-community equilibrium if and only if $\lim_{y \uparrow y^*(x_i, \rho_i)} F_i(y) \leq 1 - x_i^* \leq F_i(y^*(x_i, \rho_i))$.\(^{18}\)

4.1 Global Interactions Benchmark

Consider the following benchmark scenario. Instead of assuming that interaction effects are contained within a community, suppose that these effects are city-wide. Then each household cares only about the total number of city residents who expend high effort. Given $F$ and $\overline{p}$, define the set $X^* = \{x \in [0,1] | \lim_{y \uparrow y^*(x, \overline{p})} F(y) \leq 1 - x \leq F(y^*(x, \overline{p}))\}$. Then $\{\rho_i^*, x_i^*, Y_i^*\}_{i=1}^N$ is a ‘global interactions equilibrium’ if and only if $\rho_i^* = \overline{p}$ for all $i$, $\Sigma(x_i^*/N) \in X^*$, and the measure of $Y_i^*$ is $1/N$ for all $i$.

Under global interactions, when the $DT$ condition holds, household tenure choices cause a direct externality for all other city residents – when some households switch from renting to owning, that brings down the income threshold $y^*$ and encourages others to switch. This social multiplier effect can generate multiple equilibria.\(^{19}\) Further, since $V(.) > 0$ under $DT$, the multiple equilibria are Pareto-ranked: An equilibrium with a larger number of homeowners in the city Pareto-dominates one with a smaller number. Thus, there exists a coordination problem in tenure choice.

In effect, the above analysis shows that if households are not allowed to move across communities, then within a community, homeowners will be better citizens than renters, and a ceteris paribus increase

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\(^{18}\) The equilibrium condition allows for an atom in $F_i$ at $y^*(x_i, \rho_i)$: the largest measure of renters are all households with $y \leq y^*(x_i, \rho_i)$ (the first inequality), and all households with $y > y^*(x_i, \rho_i)$ are homeowners (the second inequality). Standard fixed-point results guarantee the existence of an equilibrium $x_i^*$ for any $\rho_i$ and $F_i$.

\(^{19}\) To see this, suppose that $F$ is continuous. Then an equilibrium $x^* \in X^*$ is given by the intersection of the curves: $y = y^*(x, \overline{p})$ and $y = F^{-1}(1-x)$. When these curves are downward sloping in the $(x, y)$ space, they can have multiple intersections, and so $X^*$ can contain multiple elements. There can be multiple equilibria whenever $y^*_x < 0$ for some $x$. 

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in the homeownership rate will improve the welfare of all residents. But households are free to locate in the community of their choice. When interaction effects are local, this has important consequences for the equilibrium tenure distribution in a city and community outcomes. This is what we now turn to.

4.2 Local Interactions Equilibria

Under local interaction effects, there exist symmetric equilibria that are $N$-fold replications of global interactions equilibria. Specifically, there exists a local interactions equilibrium with $p_i^* = \bar{p}$ and $x_i^* = x^*$ for all $i$ if and only if $x^* \in X^*$. Here, every community is a mirror-image of every other.

However, symmetric equilibria need not be ‘stable.’ Our notion of stability is analogous to that in the multi-communities literature (see e.g., Fernandez 2001, p.7): an equilibrium is stable if, starting from it, the relocation of a small mass of households from one community to another implies that under the new outcomes within these communities, the relocated households prefer to return to the original communities. [See Appendix II for a formal definition, and for the proofs of Propositions 2–5.]

Proposition 2. If $DT$ holds, then an $N$-community equilibrium in which there exist two communities $i$ and $j$ with $0 < x_i^* = x_j^* < 1$ is not stable.

Proposition 2 says that under a decreasing income threshold, a stable equilibrium under local interactions must either have all owners ($x_i^* = 1 \ \forall \ i$) or all renters ($x_i^* = 0 \ \forall \ i$), or be asymmetric. Our next result shows that if the complementarity effect is strong enough so that $SCT$ holds (subsuming $DT$), the asymmetry in tenure distribution in an $N$-community city must take a very particular form.

Proposition 3. If $SCT$ holds, then all stable equilibria exhibit tenure segregation, where homeowners and renters co-reside in at most one community. For any pair $\{i, j\}$ with $x_i^* > x_j^*$, the rental rate is higher in community $i$, and if $x_j^* > 0$, the price of homeownership $\beta^*$ is also higher in community $i$.\(^{20}\)

Complementarity in individual effort raises homeowners’ marginal willingness-to-pay for an increase in community effort vis-à-vis renters’. Whenever the former exceeds the latter, even by an

\[^{20}\text{It is also true that every tenure-segregated equilibrium in which no resident is indifferent between renting and owning within a community, is stable under SCT (the proof is available from the authors). On the other hand, if SCT}\]

\[^{20}\text{If } y^*_x > 0 \text{ for all } x, \text{ then } X^* \text{ is a singleton set. Non-emptiness of } X^* \text{ is proved by standard fixed-point arguments.}\]
infinitesimal amount (that is all that SCT requires), there will be a stable agglomeration of homeownership, and homeowner communities will have higher property values than renter communities.

We presented evidence of tenure segregation in the US in Section 1.2. Communities in the US are also segregated by income (see Jargowsky, 1997). Can the two phenomena be related? Our next result presents a sufficient condition for ‘complete segregation’, i.e., segregation by tenure and income.

**Proposition 4.** Suppose that SCI holds and that there exists a stable $N$-community equilibrium. Then there exists an equilibrium that is tenure-segregated and income-segregated: for any pair \( \{i, j\} \), if \( x_i^* > x_j^* \) then all residents in community \( i \) are richer than those in community \( j \).

When the global single crossing condition SCI holds, households segregate themselves by income solely due to the relation between income and tenure choice. While there is a close link between the forces that lead to tenure- and income-segregation, these forces are not identical. If mortgagees benefit more from an increase in community effort than self-financed owners (i.e., if SCT holds but SCI does not), then there can be an equilibrium that is segregated by tenure but not by income – where all middle-class mortgagees come together in one community, and rich homeowners co-reside with poor renters in another (an example is available from the authors). The general point is that when interaction effects exist with respect to endogenous actions, the condition for segregation of agents who choose different actions can be distinct from the condition for segregation of agents who differ in their types.

Under local interaction effects, the direct externality of tenure choice, identified in the global interactions model, leads to a within-community social multiplier effect and can generate multiple equilibria. We explore this issue with the help of an example, presented in Appendix III, of a two-community city with ‘rich’, ‘middle class’, and ‘poor’ households. Figure 2 depicts three completely segregated outcomes: the rich own homes in community 1, the poor rent in community 2, and the middle class are ‘boundary agents’ indifferent between living in either community. In outcome \( A \) (resp., does not hold, there can exist stable equilibria that are not tenure-segregated (an example is available from the authors).

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21 Regarding existence, we have the following result (proof available from the authors): If income is continuously distributed on \([y^-, y^+]\), and if SCI holds, then there exists a stable equilibrium that is completely segregated. But a continuous income distribution is not necessary for existence; see our ‘discrete’ example in Appendix III.

22 There will obviously be additional reasons for income segregation when publicly provided goods like schools are locally financed (see, for example, Fernandez and Rogerson 1996, Bénabou 1996, and Durlauf 1996).
In our example, when the middle-class income is of intermediate value and there are ‘not too many’ rich and poor households, A, B, and C co-exist as stable equilibrium outcomes (see Result 1 in Appendix III). Starting from A (resp., B), if enough middle class residents in community 1 (resp., community 2) make a tenure switch, then all of them will do so, and B (resp., C) will be reached.

However, in contrast to the global interactions case, the multiple equilibria are not necessarily Pareto-ranked on the basis of the total number of homeowners in the city. This is due to a ‘fiscal externality’ in the local interactions model – a relative increase in homeownership in a community raises its relative rental rate. Then an equilibrium $E'$ can have more homeowners than another equilibrium $E''$ and the two can be Pareto-incomparable. In our example, a move from B to C leads to an increase in the total number of homeowners, but also raises rents in community 2 so as to make homeowners indifferent between the two communities. Under SCT, this leaves the poor renters worse off in C than in B as their benefit from the improvement in community 2 civic quality is more than offset by the higher rent.

While relative rent changes can be unambiguously determined across different equilibria, absolute changes in rents cannot be so determined as they depend on the posited ‘rent normalization’ (i.e., $\rho_k = \overline{\rho}$). As a result, definitive predictions about utility changes of agents across equilibria cannot be made since utility depends on absolute rent levels. We have, however, the following result:

Proposition 5. When SCI holds, let $E'$ and $E''$ be two completely segregated equilibria with community $i$ outcomes $\{x'_i, \rho'_i\}$ and $\{x''_i, \rho''_i\}$ respectively, with $x'_i > x''_i$. If a community $i$ resident has the same utility in $E'$ and $E''$, then all households richer (resp., poorer) than that resident are better off in $E'$ (resp., $E''$). If $\rho'_i - \rho''_i \leq [q(n, x'_i) - q(n, x''_i)]$ then all community $i$ residents are better off in $E'$, and if $\rho'_i - \rho''_i \geq [q(n, x'_i) - q(n, x''_i)] + [S(x'_i) - S(x''_i)]$ then all community $i$ residents are better off in $E''$.

In the next section, we use the above result to identify winners and losers from a housing subsidy policy that expands homeownership, but affects property values in the process.

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23 See the discussion following Proposition I in Appendix III. The ambiguity in absolute rent changes is not caused by rent normalization. With vertical demand and supply of homes, if we do not normalize rents, there will be infinitely
5. Inefficiency and Policy

Given a tenure profile \( x = \{x_1, x_2, \ldots, x_N\} \), it is natural to define ‘net community quality’ for any community \( i \) as:

\[
Q(x_i) \equiv x_i[q(e, x_i) + \delta p(e, x_i) - e] + (1-x_i)[q(n, x_i) + \delta p(n, x_i) - n],
\]

and ‘net city quality’ as \( \sum_{i=1}^{N} Q(x_i) \). If net city quality is greater under a tenure profile \( x' \) than under \( x'' \), the former is more efficient in that, if the borrowing wedge \( c \) represents profits accruing to lenders, the sum of utilities of all agents – all city residents, real estate companies, and lenders – will be higher under \( x' \) than under \( x'' \).

In our model, there can be under-investment in home-buying as homeowners are not compensated for the positive externalities that they generate. This problem may be compounded by a coordination failure in tenure choice. For these reasons, there may be too few homeowners in equilibrium.

Further, note that \( Q''(x) = 2S'(x) + \{xS''(x) + q_x(n, x) + \delta p_x(n, x)\} \). While the first term is positive by the complementarity effect (this is what causes tenure segregation), the sign of the second bracketed term depends on the curvature of \( q(.) \) and \( p(.) \). If these functions are sufficiently concave in \( x \), \( Q(.) \) will be strictly concave in \( x \). Then equilibrium tenure segregation will be ‘distributionally’ inefficient, and net city quality will be improved by equalizing ownership rates across communities.

5.1 Housing Subsidy Schemes

The possibility of under-investment in homeownership immediately suggests a role for housing subsidies.\(^{25}\) Since \( Q'(x) = S(x) + xS'(x) + q_x(n, x) + \delta p_x(n, x) \), with all terms on the RHS strictly positive, a subsidy policy that alters the city tenure profile from \( x' \) to \( x'' \) in a way that the latter vector-dominates the former, will lead to an increase in net city quality and so enhance efficiency.

Consider the following subsidy scheme. Starting from a pre-subsidy equilibrium, current homeowners and real estate companies are taxed lump sum, and current renters receive a subsidy specifically
for home-buying. Subsidies can be ‘uniform’ (the same for all recipients) or ‘targeted’ (conditioned on recipient income). If a policy maker with limited information about the magnitude of local interaction effects and income distribution implements such a scheme, will the city tenure profile necessarily improve? Will all households necessarily gain? Will it be cheaper to give targeted subsidies?

We address these questions using our two-community example. Starting from outcome \( A \), we determine what can be achieved by giving increasing levels of subsidies when SCI holds and when the tax-burden on the rich is not so large that they switch to renting. We identify the following features of housing subsidy policies. [See Results 1-3 in Appendix III and the discussion following them.]

(1) **Improving Tenure Profile:** As housing subsidy amounts cross successively higher thresholds, the city tenure profile improves from \( A \) to \( B \) to \( C \) (with each profile vector-dominating the preceding one). But tenure improvement may not be ‘continuous’ in subsidies – the post-policy outcome for a subsidy incrementally below a threshold can be much inferior to that for a subsidy just above it.\(^{26}\) Further, whether a renter household finds it worthwhile to take the housing subsidy and switch to owning depends on the number of other renters who do so. So, post-subsidy ownership rates can still be low if there is a coordination failure. Note that non-pecuniary policy interventions that change the expectations of sufficiently many residents can solve this problem.\(^{27}\) But if they fail to do so, larger subsidies will be required to solve the coordination problem and to ensure that a desired tenure profile is attained.

(2) **Generating Winners and Losers:** Due to the fiscal externality in tenure choice, housing subsidies, while improving tenure profiles, can alter rental rates in such a way as to hurt some city residents – even ones not being taxed to finance the subsidy. In our example, all city residents can gain under a subsidy-driven move from \( A \) to \( B \) – there is a strict utility gain for all middle class and poor households, and the rich will also gain if the tax burden on them is not too large and if they care *enough* about community

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\(^{26}\) In our example, threshold effects arise because the income distribution is discrete. In the real world, the fact that most housing tenure contracts are 0-1, offering either 0 or 100% ownership, will also generate threshold effects. As indicated in the Introduction, policy makers seem to recognize the existence of such threshold effects.

\(^{27}\) The following are two recent examples. Two non-profit organizations started a program in a Baltimore neighborhood that guarantees the value of a house no matter how much market prices may drop (*New York Times*, 6/13/99, pp. 1, 34). In the UK, in an effort to erase associations with its past, authorities planned to rename the place names in a Newcastle neighborhood that had suffered from high crime and abandonment (*The Economist*, 6/26/99, p. 64).
quality. But if the subsidy level is increased further so that the city moves from B to C, the utility changes are reversed – while the middle class neither gains nor loses from the move, the rich are worse off because of the tax burden, and the poor are worse off because of the increase in rents.

Because of the fiscal externality, household utility can change non-monotonically with subsidy-induced improvements in tenure profile. Without detailed knowledge of the ‘city parameters,’ it is not possible to predict the precise welfare changes of city residents for any given level of subsidy. However, Proposition 5 allows us to conclude that (apart from the welfare loss of the rich due to the tax burden): (i) a subsidy-induced increase in property values in a community is most likely to hurt the poorest residents, especially if they continue to rent in the post-subsidy equilibrium, and (ii) if the poorest residents do not lose post-subsidy, then all community residents gain.

(3) Targeted Subsidies: If subsidies can be conditioned on recipients’ incomes, then a desired tenure profile can be achieved at a lower cost. In our example, the ‘all owners \( \{x_i = 1 \; \forall \; i\} \)’ outcome can be attained with a smaller aggregate subsidy bill under targeted subsidies than under uniform subsidies. This is because a targeted subsidy scheme can utilize the within-community social multiplier. In our example, the targeted subsidy policy pulls up the middle class into homeownership, and then gives the minimal subsidy that is necessary to induce the poor to own as well. The scheme demonstrates that it can be more effective to give a moderate subsidy to both middle- and low-income households than a large one to the latter, even if the social objective function counts only the welfare of the latter.28

5.2 Desegregation Policies

When tenure segregation is inefficient, i.e., when net community quality is concave in community effort, the aim of a corrective policy is to encourage homeowners to ‘accept’ renters as their community neighbors. We now present a tax-subsidy scheme that can induce ‘stable desegregation.’

Let \( \bar{x}^* < 1 \) be the maximal element of \( \bar{X}^* \) (the set of global interactions equilibria), and suppose that the tenure profile \( \{x_i = \bar{x}^* \; \forall \; i\} \) is more efficient than the ‘best’ asymmetric equilibrium tenure

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28 The informational demands of targeted subsidies are more than those of a uniform subsidy scheme. To design the least-cost targeted subsidy scheme, a policy maker needs to know not only a recipient’s income class, but also the income threshold for home-buying for that income class.
profile. Further, suppose that $DT$ holds so that the symmetric equilibrium is unstable. Then, how can the symmetric tenure profile be turned into the unique stable post-intervention equilibrium?

Consider the following tax-subsidy scheme: Within each community, if $x$ fraction of residents own their homes, each owner is taxed a lump sum $\tau(x) = \lambda(x - \bar{x}^*)$ for some $\lambda > 0$, and each renter is subsidized a lump sum $\sigma(x) \equiv (x/1-x)\tau(x)$. Note that there will never be any budget deficit under the scheme (for $x = 1$, the tax collected from homeowners can be spent in any non-distortionary manner).

When the ownership rate $x$ in a community is above the ‘target’ $\bar{x}^*$, the scheme reduces (resp., increases) an homeowner’s (resp. renter’s) disposable income and lowers (resp., raises) its marginal benefit from an increase in $x$. It does the opposite when $x < \bar{x}^*$ by taxing renters and subsidizing owners. Then, if the tax structure is sufficiently steep, i.e., if $\lambda$ is large enough, the scheme can ensure that, post-intervention, (i) renters value an increase in $x$ no less than homeowners around the target profile $\{x_i^* = \bar{x}^* \forall i\}$ so that it becomes a stable equilibrium outcome, and (ii) no segregated outcome remains a stable equilibrium. In Appendix III, Result 4 shows how this can be achieved in our example. The scheme requires us to identify the efficient symmetric equilibrium tenure profile. But once that is done, it can be implemented by choosing $\lambda$ sufficiently large. An appealing feature of the scheme is that when it is successful, no taxes are paid in equilibrium and no subsidies are received.

Policies to expand homeownership and those to induce desegregation operate at different margins. A housing subsidy policy expands homeownership, but when the pre-policy equilibrium is income-segregated, it does not involve relocation of households across communities. In contrast, a desegregation policy does not necessarily create new homeowners, but induces households to relocate so that owners and renters co-reside in each community. As a result, the identities of the winners and losers can be very different under the two policies. Under the former, the losers are likely to be the rich pre-subsidy owners (due to the tax burden) and the poor post-subsidy renters (because of higher rents), and the ‘new’ middle class homeowners are most likely to gain. On the other hand, all renters are likely to be better off under desegregation, and all owners worse off. To the extent that the home-owning middle class has significant influence on policy making (as they are the likely to be the ‘median voters’), our analysis suggests that housing subsidy schemes will be easier to implement than desegregation policies.

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6. Conclusion

A key feature of a healthy community is that residents are proactive participants in community institutions. This paper presents a community-interactions model where externalities arising from non-contractible individual effort produce concentrations of low-income households in disadvantaged renter communities in which residents lack the incentive to be proactive. In our model, all households desire to be homeowners and be responsive citizens, but credit market imperfections force the poorer ones to rent. All households also want to live near homeowners because they generate positive externalities. But homeowners may outbid renters for land in communities with a high proportion of homeowners, leading to tenure segregation. An interplay of within-community externalities and market forces can create ‘good’ and ‘bad’ citizens out of ex ante similar households and then clump each group together.

Our analysis explains the significant segregation of homeowners and renters across communities in the US, and the fact that poor renter communities have much worse civic environments than rich homeowner communities. The model also provides a framework to study policy intervention in the housing market. We show how different tax-subsidy schemes can improve the city tenure profile and induce co-residence of owners and renters. By determining the winners and losers under alternative tax-subsidy policies, we identify the sources of potential political opposition to such policies.

A limitation of our work is that it is essentially static. In the real world, the process of spatial arbitrage that we treat as instantaneous, plays out over time. Intertemporally, community interaction effects have the potential of magnifying small changes in individual behavior and thus generating large changes in aggregate community quality. Then a small policy intervention can achieve remarkable results in improving a neighborhood. However, our framework does provide a useful starting point for a dynamic analysis of the impact of a government-sponsored homeownership program on the time path of housing prices, homeownership rates, and improvements in community civic environment.

29 An example of this is the turn-around of Charlotte Gardens in the South Bronx that is referred to in the New York Times editorial quoted at the beginning of our paper. In the 1970’s, the South Bronx was “the definition of blight, nearly destroyed by poverty, crime, and arson” (New York Times, 11/2/1997). With money from New York City, 89 single-family homes were built in Charlotte Gardens in the mid-1980’s, and sold for $49,500-$60,000 to low-income families who agreed not to sell their homes for ten years. Mayor Ed Koch pronounced that the new owners would “defend these houses with their lives.” By 1997, their value had risen to $185,000, private construction had increased, and property values had risen all over the South Bronx.
Appendix I: An Agency Model of Tenure Contracting

The contracting model presented in the text contains two critical simplifying assumptions: (i) tenure contracts have to be linear in the observable outcome – the future price of a home, and (ii) this price is a deterministic function of unobservable effort. In what follows, we briefly present a more general principal-agent model of tenure contracting between a household and a real estate company.

A long-lived risk-neutral principal (real estate company) owns a durable good $H$ (housing unit). An agent (household) lives for two periods and benefits from consuming the flow of services from $H$ only in the first period. In that period, the agent can put in effort to add value to $H$, which benefits her and increases the future price of $H$ (this price goes to the principal). Both players consume a divisible numeraire commodity in all periods, and discount the future by $\delta \in (0, 1)$.

The agent’s effort ($a$) can be high ($e$) or low ($n$). It is not observable by the principal and so cannot be contracted upon. The agent’s current benefit from effort net of cost is $q(a) - a$. The future price of $H$ is a random variable $P$ distributed on $[0, \infty)$ according to $G(p|a)$, where $G(p|e)$ first-order stochastically dominates $G(p|n)$. A feasible contract is a pair $\{\alpha(p), \beta\}$, where $\beta \in \mathbb{R}$ is the ‘up-front payment’ that the agent makes to the principal, and $\alpha(p)$ is the ‘rebate’ that the principal gives back to the agent in the second period if the realized future price of $H$ is $p$. The rebate function $\alpha(p)$ can be any real-valued function, but it is required to satisfy the ‘limited liability clause’ $\alpha(p) \geq 0$ for all $p$. The contract $\{\alpha, \beta\}$ is thus a specific ‘complete contract with limited liability’ under moral hazard.

Given $\{\alpha, \beta\}$, if the agent (with current income $y$ and future income $w$) chooses effort $a$ and borrows $b$, the principal’s utility is $\pi(a; \alpha, \beta) = \beta + \delta \int_0^\infty [p - \alpha(p)]dG(p \mid a)$, and the agent’s utility is:

$$u(a, b; \alpha, \beta \mid y) =
\begin{cases}
[y - \beta + b] + [q(a) - a] + \delta \int_0^\infty [w - (1 + rB)b + \alpha(p)]dG(p \mid a) & \text{if } y - \beta + b \geq 0, \\
-\infty & \text{otherwise},
\end{cases}$$

where the borrowing wedge $[\delta(1+r_B) - 1]$ is strictly positive.

Let effort level $\alpha^*(\beta, \alpha \mid y)$ and debt level $b^*(\beta, \alpha \mid y)$ maximize $u(\cdot \mid y)$ under the contract $\{\alpha, \beta\}$. Assume the existence of the following incentive problem: (i) if $\alpha(p) = 0$ for all $p$, then $\alpha^* = n$ for all $y$, and (ii) if $\alpha(p) = p$ for all $p$, then $\alpha^* = e$ for all $y$. Assume further that the players have the right to the default rental contract $\{\alpha(p) = 0 \ \forall \ p, \ \beta = \rho\}$. This contract pins down the players’ reservation payoffs:
for the principal, \( \pi^0 = \rho + \delta \int_0^\infty pdG(p \mid n) \); and for the agent, \( u^0(y) = [y - \rho] + [q(n) - n] + \delta w \).

Consider the model where the agent makes a take-it-or-leave-it contract offer. Here the optimal contract solves the following problem: maximize \( u(a, b; \alpha, \beta \mid y) \) with respect to \( a, b, \alpha(\cdot), \) and \( \beta \), subject to: (i) \( a = a^*(\alpha, \beta \mid y) \) and \( b = b^*(\alpha, \beta \mid y) \) [incentive compatibility]; (ii) \( \pi(a^*(\cdot); \alpha, \beta) \geq \pi^0 \) [individual rationality]; and (iii) \( \alpha(p) \geq 0 \) for all \( p \) [limited liability].

The solution to the above problem will have the following features. There will exist a threshold income level \( y^*(\rho) \) such that, if the agent’s current income \( y \) is less than the threshold, the optimal contract will be the default contract and \( a^* = n \); and if \( y > y^* \), the optimal contract will generate \( a^* = e \).

Thus there will be a wealth effect on incentives. The moral hazard problem will not be ‘solved’ for all agents (i.e., for all \( y \)) due to (i) the incentive problem, (ii) the agents’ desire to smooth consumption, (iii) the limited liability clause, and (iv) the borrowing wedge. A similar result will hold in the alternative model where the principal makes a take-it-or-leave-it contract offer.

The above discussion clarifies the nature of the moral hazard problem in our model, and demonstrates the robustness of our results. The analysis seems to suggest the necessity of a limited liability clause to generate wealth effect on incentives. However, consider the following ‘extended’ model:

The agent lives for three periods, consumes \( H \) only in the first period, and consumes the numeraire in all periods. A feasible contract \( \{\alpha, \beta\} \) no longer has to satisfy a limited liability clause, i.e., \( \alpha(p) \) can be negative for some \( p \). The agent can borrow \( b_t \) in period \( t = 1, 2 \), under the same terms as before. Here, the agent will be forced to borrow in period 2 if \( \alpha(p) \) is a large negative number to ensure non-negative consumption in period 2. Then the optimal contract will exhibit a similar wealth effect on incentives. The reason for this is that incentive payments are effectively bounded below because the agent will not accept a contract under which his income falls below zero in any period.

**Appendix II: Proofs of Propositions 2–5**

We begin by defining ‘stability’. Fix an equilibrium \( E \), and take any community pair \( \{i, j\} \). Then for any \( y^i \in Y_i^* \) and \( y^j \in Y_j^* \), \( [V(y^i, x^i, \rho_i^*) - V(y^i, x^j, \rho_j^*)] - [V(y^j, x^i, \rho_i^*) - V(y^j, x^j, \rho_j^*)] \geq 0 \). Construct an ‘\( \varepsilon \)-switch’ as follows. Find a subset \( Y(\varepsilon) \) of \( Y_i^* \) of measure \( \varepsilon > 0 \) such that all households in \( Y(\varepsilon) \) would make identical tenure choices in \( i \) and in \( j \); similarly, find a subset \( Y(\varepsilon) \) of \( Y_j^* \). Holding \( \rho_i^* \) and \( \rho_j^* \) fixed, relocate the households in \( Y(\varepsilon) \) to \( j \) and those in \( Y(\varepsilon) \) to \( i \). Let \( x(\varepsilon) \) (resp. \( x(\varepsilon) \)) be the
post-switch tenure outcome in \(i\) (resp., \(j\)) when all old residents in \(i\) (resp., \(j\)) make the same tenure choice as before and the migrants in \(i\) (resp., \(j\)) respond optimally to \((x_i^*, \rho_i^*)\) (resp., \((x_j^*, \rho_j^*)\)). If the condition: 
\[
[V(y', x_i(\varepsilon), \rho_i^*) - V(y', x_j(\varepsilon), \rho_j^*)] - [V(y'', x_i(\varepsilon), \rho_i^*) - V(y'', x_j(\varepsilon), \rho_j^*)] \geq 0 \quad \text{for all } y' \in Y_i(\varepsilon) \text{ and } y'' \in Y_j(\varepsilon),
\]
holds for all \(\varepsilon\)-switches for \(\varepsilon\) small, and for all \(\{i,j\}\), then \(E\) is (locally) stable.\(^{30}\)

Next, we establish the following claim that is used in our proofs. To simplify the notation, let \(y_i^* = y_i^*(x_i^*, \rho_i^*), \beta_i^* = \beta_i^*(x_i^*, \rho_i^*), q_i^* = q(n, x_i^*),\) and \(S_i^* = S(x_i^*)\). From (5) and (6), note that \(V(y) = u''(y, x_i, \rho_i)\) for \(y \leq y^*(x_i, \rho_i)\), and \(V(y) = u''(y, x_i, \rho_i) + \min\{c(y - y^*(x_i, \rho_i)), S(x_i)\}\) for \(y > y^*(x_i, \rho_i)\).

**Claim.** (a) When \(SCT\) holds, if \(x_i^* > x_j^*\) and \(\rho_i^* - \rho_j^* \leq q_j^* - q_i^*\), then \(y_i^* < y_j^*\).

(b) When \(SCI\) holds, if \(x_i^* > x_j^*\) and \(\rho_i^* - \rho_j^* \geq (q_i^* - q_j^*) + (S_i^* - S_j^*)\), then \(\beta_i^* > \beta_j^*\).

**Proof:** Note that \(y_j^* - y_i^* = -[\int_{y_i^*}^{y_j^*} [y(x_i^*, \rho_i^*) - y_j^*] - [\rho_i^* - \rho_j^*]] dx - [\rho_i^* - \rho_j^*]\). By \(SCT\), this is strictly greater than \([q_i^* - q_j^*] - [\rho_i^* - \rho_j^*]\), proving (a). Part (b) is proved similarly.

**Proof of Proposition 2:** Consider an equilibrium where there is a community pair \(\{i, j\}\) with \(0 < x_i^* = x_j^* < 1\). Then \(\rho_i^* = \rho_j^*\), and so \(y_i^* = y_j^*\). Consider an \(\varepsilon\)-switch as described above where \(y' > y_i^* = y_j^* > y''\) for all \(y' \in Y_i(\varepsilon)\) and \(y'' \in Y_j(\varepsilon)\). After the switch, the migrants to \(i\) (resp., \(j\)) will rent (resp., own) implying that \(x_i(\varepsilon) < x_i^* < x_j(\varepsilon)\). Then \(V(y', x_i(\varepsilon), \rho_i^*) - V(y', x_j(\varepsilon), \rho_j^*)] - [V(y'', x_i(\varepsilon), \rho_i^*) - V(y'', x_j(\varepsilon), \rho_j^*)]) = -\int_{x_i(\varepsilon)}^{x_j(\varepsilon)} [V_i(y', x_i^*, \rho_i^*) - V_i(y'', x_j^*, \rho_j^*)] dx\), which is strictly negative under \(DT\) for any \(y' \in Y_i(\varepsilon)\) and \(y'' \in Y_j(\varepsilon)\) and \(\varepsilon > 0\). Thus an equilibrium with \(0 < x_i^* = x_j^* < 1\) is unstable under \(DT\).

**Proof of Proposition 3:** Suppose that \(E\) is a stable equilibrium that is not tenure-segregated. Then there is a pair \(\{i,j\}\) with \(x_i^* \in (0, 1)\) and \(x_j^* \in (0, 1)\). Since \(SCT\) subsumes \(DT\), stability implies that \(x_i^* \neq x_j^*\).

Suppose (w.l.o.g.) that \(1 > x_i^* > x_j^* > 0\). Since there are renters in \(i\) and in \(j\), \(\rho_i^* - \rho_j^* = q_j^* - q_i^*\). Then \(y_i^* < y_j^*\) by Claim (a). This implies that for all \(y \in (y_i^*, y_j^*)\), \(V(y) > u''(y, x_i^*, \rho_i^*) = u''(y, x_j^*, \rho_j^*) = V(y),\) and that for all \(y > y_j^*\), \(V(y) = u''(y, x_i^*, \rho_i^*) + \min\{c(y - y_i^*), S_i^*\} > u''(y, x_j^*, \rho_j^*) + \min\{c(y - y_j^*}, S_j^*\}\)

\(^{30}\) If there were a finite number of households, we would check for stability by relocating one household, and it would obviously make a unique tenure choice in a community. That is why we require all households in \(Y(\varepsilon)\) to make identical tenure choices in \(i\) and in \(j\). Further, instead of using \(x_i(\varepsilon)\), we could work with \(x_i(\varepsilon)\) where \(x_i(\varepsilon)\) is a post-switch equilibrium in \(i\) given \(\rho_i^*\). For any given \(\varepsilon\)-switch, whether the inequality required for stability holds or not depends on the signs of \([x_i^*(\varepsilon) - x_i^*]\) and \([x_j^*(\varepsilon) - x_j^*]\). If \(x_i^*(\varepsilon)\) is unique for \(l = i, j\), then \([x_i^*(\varepsilon) - x_i^*]\) will have the same sign as \([x_j^*(\varepsilon) - x_j^*]\), and so the two definitions will give the same results. Even if there are multiple post-switch equilibria, there will be at least one equilibrium in each community \(l\) where \([x_i^*(\varepsilon) - x_i^*]\) has the same sign as \([x_j^*(\varepsilon) - x_j^*]\).
obeys in that can be no owners in. So E must be tenure segregated.

Regarding housing prices in the two communities, \( x_i^* > x_j^* \) implies that \( \rho_i^* > \rho_j^* \), since otherwise the renters in \( j \) will move to \( i \). When \( x_j^* > 0 \), it must be that \( y_i^* \geq y_j^* \), since otherwise there can be no owners in \( j \). By (5), \( x_i^* > x_j^* \) and \( y_i^* \geq y_j^* \) implies that \( \beta_i^* > \beta_j^* \), and Proposition 3 is established.

**Proof of Proposition 4:** Let \( E \) be a stable equilibrium, and take any \( \{i, j\} \) in \( E \) with \( x_i^* > x_j^* \). Since SCI subsumes \( SCT \), \( E \) is tenure segregated. Then there are three cases: (i) \( 1 = x_i^* > x_j^* = 0 \), (ii) \( 1 > x_i^* > x_j^* = 0 \), and (iii) \( 1 = x_i^* > x_j^* > 0 \). In case (i), suppose that \( y' > y'' \) and that \( y' \) lives in \( j \) and \( y'' \) in \( i \). Then \( y' \) must prefer to rent in \( j \) than own in \( i \), and \( y'' \) must prefer to own in \( i \) than rent in \( j \), i.e., \( \min\{c(y'' - y_i^*), S_i^*\} \geq (\rho_i^* - \beta_i^*) - (q_i^* - q_j^*) \geq \min\{c(y' - y_i^*), S_i^*\} \). This inequality can be satisfied if and only if \( y'' \geq \beta_i^* \), and in that case, \( \rho_i^* - \beta_i^* = q_i^* - q_j^* + S_i^* \). But then, \( \beta_i^* > \beta_j^* \) by SCI and Claim (b), which implies that \( y' > y'' \geq \beta_i^* > \beta_j^* \). Then \( y' \) strictly prefers to own in \( j \) which contradicts our supposition that \( x_j^* = 0 \). Thus, when \( x_j^* = 1 \) and \( x_j^* = 0 \), residents in \( i \) are richer than those in \( j \).

In case (ii), it must be that \( \rho_i^* - \beta_i^* = q_i^* - q_j^*, y_i^* < y_j^* \), and all households with \( y > y_i^* \) strictly prefer to live in \( i \). So, if \( y' > y'' \), and \( y' \) lives in \( j \) while \( y'' \) lives in \( i \), both must rent and so be indifferent between \( i \) and \( j \). In case (iii), it can be proved using similar arguments that for any \( y' > y'' \), either it cannot be that \( y' \) lives in \( j \) and \( y'' \) lives in \( i \), or it must be that \( y' \) and \( y'' \) are indifferent to living in \( i \) and \( j \). When they are indifferent, \( y' \) can be moved to \( i \) and \( y'' \) can be moved to \( j \) without disturbing any equilibrium conditions. So if a stable equilibrium exists, there must be one that is completely segregated.

**Proof of Proposition 5:** Since \( E' \) and \( E'' \) are completely segregated, the set of residents in \( i \) (\( Y_i^* \)) is the same in both. Our first claim follows directly from SCI. Consider the poorest resident in \( i \), who necessarily rents in \( E'' \). When \( \rho_i' - \rho_i'' \leq [q(n, x_i') - q(n, x_i'')] \), it is better off in \( E' \) whether it rents or owns in \( E' \). Then all residents in \( i \) are better off in \( E' \). Next, consider the richest resident in \( i \), who necessarily owns in \( E' \). When \( \rho_i' - \rho_i'' \geq [q(n, x_i') - q(n, x_i'')] + [S(x_i') - S(x_i'')] \), it is worse off in \( E' \) whether it owns or rents in \( E'' \) since \( \beta^*(x_i', \rho_i') > \beta^*(x_i'', \rho_i'') \) under SCI. Then all residents in \( i \) are worse off in \( E' \).

**Appendix III:** *An Example of a Two-community City*

Consider a city with two communities, each with homes of measure half. There is \( \mu \) measure of ‘rich’
households each with income $y^H$, the ‘middle class’ is of measure $\mu^M$ each with income $y^M$, and there is $\mu^L$ measure of ‘poor’ households each with income $y^L$ (with $\mu^H+\mu^M+\mu^L=1$). We posit that the $q(.)$ and the $p(.)$ functions are such that SCI holds. Community 1 rental rate is pegged at $\bar{\rho}$.

Let $\bar{y}^* \equiv y^*(1, \bar{\rho})$ and $\bar{\beta}^* \equiv \beta^*(1, \bar{\rho})$. Define $\rho^0(y) \equiv \bar{\rho} - \left[q(n, 1) - q(n, 0)\right] - c[y - \bar{y}^*]$. Under SCI, there exists a unique $y^0 \in (\bar{y}^*, y(0, \bar{\rho}))$ such that $y^0 = y^*(0, \rho^0(y^0))$. Let $\beta^0 \equiv \beta^*(0, \rho^0(y^0))$. Then, $\bar{y}^* < y^0 < \beta^0 < \bar{\beta}^*$. Next, define $\bar{\mu}$ such that $y^0 = y^*(2\bar{\mu}, \bar{\rho})$. Finally, define $\hat{\rho}(\mu) \equiv \bar{\rho} - [q(n, 1) - q(n, 1-2\mu)] - c[y^*(1-2\mu, \hat{\rho}(\mu)) - \bar{y}^*]$. Note that for $y \in (\bar{y}^*, y^0)$, there exists a unique $\hat{\mu}(y) \in (0, \frac{1}{2})$ such that $y = y^*(1-2\hat{\mu}(y), \hat{\rho}(\hat{\mu}(y)))$.

We assume that (i) the rich always own and the poor always rent, (ii) the middle class income is the median income, and (iii) if a middle class household ‘buys’ a home, it has to take out a mortgage:

**Parameter restriction $[R]$:** (i) $y^L < y^* < y^*(0, \bar{\rho}) < y^H$, (ii) $\mu^0 \in (0, \frac{1}{2})$ for $\theta = L, H$, and (iii) $y^M < \beta^0$.

Supposing that $x_1 \geq x_2$ (w.l.o.g.), $A, B$, and $C$ are the only completely segregated outcomes under $[R]$. 

**Result 1.** Under $[R]$ and the normalization $\rho_1 = \bar{\rho}$: (i) $A$ is a stable equilibrium outcome if and only if $y^M < y^*(2\mu^H, \bar{\rho})$; (ii) $B$ is a stable equilibrium outcome if and only if $\bar{y}^* < y^M < y^0$; and (iii) $C$ is a stable equilibrium outcome if and only if either $\{y^0 < y^M\}$ or $\{\bar{y}^* < y^M < y^0 \text{ and } \mu^L < \hat{\mu}(y^M)\}$.

**Proof:** Let $\rho_1(O)$ be the equilibrium rental rate in $i$ in outcome $O$. (i) For $A$ to be equilibrium, $y^M$ must be indifferent between renting in 1 and in 2, requiring that $\rho_1(A) - \rho_2(A) = [q(n, 2\mu^H) - q(n, 0)]$. Then $y^M$ will strictly prefer to rent if and only if $y^M < y^*(2\mu^H, \bar{\rho})$. Here and subsequently, strict preference is required for stability. (ii) For $B$ to be equilibrium, $y^M$ must be indifferent between being a mortgagee in 1 and renting in 2, requiring that $\rho_1(B) - \rho_2(B) = [q(n, 1) - q(n, 0)] + c[y^M - \bar{y}^*]$. Then $y^M$ will strictly prefer to own in 1 if and only if $y^M > \bar{y}^*$ and to rent in 2 if and only if $y^M < y^*(0, \rho_2(B)) = y^0$. (iii) For $C$ to be equilibrium, $y^M$ must be indifferent between being a mortgagee in 1 and in 2, requiring that $\rho_1(B) - \rho_2(B) = [q(n, 1) - q(n, 0)] + c[y^*(1-2\mu^L, \hat{\rho}(\mu^L)) - \bar{y}^*]$. Then $y^M$ will strictly prefer to own in 1 if and only if $y^M > \bar{y}^*$ and to own in 2 if and only if $y^M > y^*(1-2\mu^L, \hat{\rho}(\mu^L))$. The last condition is satisfied if and only if either $\{y^0 < y^M\}$ or $\{y^M < y^0 \text{ and } \mu^L < \hat{\mu}(y^M)\}$.

Result 1 shows that given $\rho_1 = \bar{\rho}$, $A, B$, and $C$ co-exist as stable equilibria when, in addition to $[R]$,
y^M \in (\bar{y}^*, y^0), \mu^H \in (0, \bar{\mu}), \text{ and } \mu^L \in (0, \hat{\mu}(y^M)). \text{ Defining } V^\theta(O) \text{ to be the equilibrium payoff to household } y^\theta (\theta = H, M, L) \text{ in outcome } O, \text{ note that when } \rho_1 = \bar{\rho}:

\begin{align*}
V^H(A) &= u^\sigma(y^H, 2\mu^H, \bar{\rho}) + \min \{c(y^H - y^\mu(2\mu^H, \bar{\rho})), S(2\mu^H)\} < V^H(B) = u^\sigma(y^H, 1, \bar{\rho}) + \min \{c(y^H - \bar{y}^*), S(1)\}; \\
V^M(A) &= u^\sigma(y^M, 2\mu^H, \bar{\rho}) < V^M(B) = V^M(C) = u^\sigma(y^M, 1, \bar{\rho}) + c(y^M - \bar{y}^*) \text{; and} \\
V^L(A) &= u^\sigma(y^L, 2\mu^H, \bar{\rho}) < V^L(C) = u^\sigma(y^L, 1, \bar{\rho}) + c[y^*(1 - 2\mu^L, \hat{\rho}(\mu^L)) - \bar{y}^*] < V^L(B) = u^\sigma(y^L, 1, \bar{\rho}) + c(y^M - \bar{y}^*).
\end{align*}

A move from A to B improves the quality of community 1 and raises \rho_1 relative to \rho_2; a move from B to C improves the quality of community 2 and raises \rho_2 relative to \rho_1. Under the rent normalization \rho_1 = \bar{\rho}, \text{ the rich and the middle class gain in a move from } A \text{ to } B \text{ and are indifferent in moving from } B \text{ to } C, \text{ the poor gain in a move from } A \text{ to } B \text{ and lose in a move from } B \text{ to } C, \text{ and the real estate companies lose in a move from } A \text{ to } B \text{ and gain in a move from } B \text{ to } C.

The changes in agents’ utility across the three outcomes (when they are all equilibria) do depend on the rent normalization. If \rho_2 is pegged at \bar{\rho}, \text{ there exist alternative parameter configurations for which } A, B, \text{ and } C \text{ are all stable equilibria. Then the rich will gain in a move from } A \text{ to } B \text{ and from } B \text{ to } C, \text{ the middle class and the poor will be indifferent in moving from } A \text{ to } B \text{ and will gain in a move from } B \text{ to } C, \text{ and the real estate companies will gain (resp., lose) in a move from } A \text{ to } B \text{ (resp., } B \text{ to } C).

We now study the effects of uniform housing subsidies. In addition to [R], \text{ we assume that: (i) } y^M < \bar{y}^*, \text{ (ii) } \mu^H \in (\bar{\mu}, \frac{1}{2}) \text{ so that } \bar{y}^* < y^*(2\mu^H, \bar{\rho}) < y^0, \text{ (iii) } \bar{y}^* - y^L > y^0 - y^M, \text{ and (iv) there exists } \tilde{y} \in (y^*(2\mu^H, \bar{\rho}), y^0) \text{ such that } \mu^L = \hat{\mu}(\tilde{y}) \text{ and } \tilde{y} - y^L < (y^0 - y^M)/(1 + c). \text{ Then by Result 1, outcome } A \text{ is the only pre-subsidy stable equilibrium. Define the following successively increasing ‘subsidy thresholds’:}

\sigma^{(1)} = \bar{y}^* - y^M, \sigma^{(2)} = y^*(2\mu^H, \bar{\rho}) - y^M, \sigma^{(3)} = \tilde{y} - y^M, \text{ and } \sigma^{(4)} = (y^0 - y^M)/(1 + c).

**Result 2.** Suppose that the uniform subsidy amount \sigma is financed in a way that the post-tax income of the rich is greater than \allowbreak y^*(0, \bar{\rho}). \text{ Let } \Xi \text{ be the set of post-subsidy stable equilibria. Then: (1) for } \sigma < \sigma^{(1)}, \Xi = \{A\}; \text{ (2) for } \sigma \in (\sigma^{(1)}, \sigma^{(2)}), \Xi = \{A, B\}; \text{ (3) for } \sigma \in (\sigma^{(2)}, \sigma^{(3)}), \Xi = \{B\}; \text{ (4) for } \sigma \in (\sigma^{(3)}, \sigma^{(4)}), \Xi = \{B, C\}; \text{ and (5) for } \sigma \in (\sigma^{(4)}, y^0 - y^M \}, \Xi = \{C\}.

**Proof:** Similar arguments as in Result 1 prove that: (i) \text{ A is a post-subsidy stable equilibrium (with the same rental rates as under ‘no subsidy’) if and only if } \sigma < \sigma^{(2)}, \text{ and (ii) } C \text{ is a post-subsidy stable
equilibrium (with the same rental rates as under no subsidy), where all middle class households buy homes with subsidy, if \( \sigma \in (\sigma^3, y^0 - y^M) \) and only if \( \sigma > \sigma^3 \). Now consider the post-subsidy outcome \( B \), where \( y^M \) buys a home with subsidy in 1, and rents in 2. Then given \( \rho_1 = \bar{\rho} \), indifference of \( y^M \) requires \( \rho_2 = \rho_2(B) - (1+c)\sigma \) (\( \rho_2(B) \) as defined above). At these rents, \( y^M \) strictly prefers to own in 1 if and only if \( y^M + \sigma > \bar{\gamma}^* \) and strictly prefers to rent in 2 if and only if \( y^M < y^*(0, \rho_2) = y^0 - (1+c)\sigma \). These conditions are satisfied if and only if \( \sigma \in (\sigma^1, \sigma^4) \). In \( B \), \( \rho_2 \) is lower post-subsidy than in the case of ‘no subsidies’ so as to make \( y^M \) indifferent between renting in 2 and owning (with subsidy) in 1.

Thus, there are discrete improvements in the set of post-subsidy equilibria as \( \sigma \) crosses different thresholds. Further, higher subsidies are needed to solve the coordination problem: when \( \sigma \in (\sigma^1, \sigma^2) \), while \( B \) is ‘attainable,’ the city may be stuck in \( A \); this is solved by raising \( \sigma \) above \( \sigma^2 \).

Comparing household utility across the post-subsidy outcomes (for \( \rho_1 = \bar{\rho} \)), all middle class and poor households are strictly better off in \( B \) than in \( A \); the middle class in community 1 gain from being subsidy-financed homeowners, and those in community 2 gain from the post-subsidy rent decrease. Then, if the ‘tax burden’ on the rich is not too large (i.e., a large part of the funds for subsidy can be obtained by taxing the real estate companies), and if they care enough about civic quality (i.e., \( V_H(x) \gg V_M(x) \)), the rich are also better off in \( B \). In contrast, no household is better off when the post-subsidy outcome is \( C \) rather than \( B \); while the middle class is indifferent, the rich are worse off because of the tax burden, and the poor are worse off because of the increase in community 2 rent.

Next, we consider targeted subsidies where the middle class and the poor are given subsidies \( \sigma^M \) and \( \sigma^L \), respectively. Suppose that \( [R] \) holds, \( y^M < \bar{\gamma}^* \), and \( \mu^M \leq \mu^L \). Then \( A \) is the only stable pre-subsidy equilibrium. Consider the minimal subsidies needed to attain the ‘all owners \{x_1 = x_2 = 1\}’ outcome as the only post-subsidy equilibrium. It is easy to see that the middle class and the poor will be better off under this outcome. The rich will also be better of provided the tax burden is not too large and they care enough about civic quality. Define \( \hat{y}^* = y^*(1-2\mu^L, \hat{\rho} (\mu^L)) \) and note that \( \hat{y}^* \in (\bar{\gamma}^*, y^0) \).

**Result 3.** Suppose that the post-tax income of the rich is always greater than \( y^*(0, \bar{\rho}) \). Then, to attain \( x_1 = x_2 = 1 \) as the unique post-subsidy equilibrium, the least-cost uniform subsidy scheme (i.e., the one with the smallest total subsidy bill) must set \( \sigma = \max \{y^0 - y^M, \hat{y}^* - y^L \} \), while the least-cost targeted subsidy scheme must set \( \sigma^M = y^0 - y^M \) and \( \sigma^L = \hat{y}^* - y^L \).

**Proof:** Let \( z^M \) be the post-subsidy median income and \( z^L \) the post-subsidy low income. If \( z^M \geq y^0 \) and \( z^L \geq \hat{y}^* \)
≥ \hat{y}^* \text{, then } \{x_1 = x_2 = 1\} \text{ is a post-subsidy equilibrium outcome, and giving slightly higher subsidies will make it stable. But if either } z^M < y^0 \text{ or } z^L < \hat{y}^* \text{ or both, one of the segregated outcomes } A, \text{ or } B, \text{ or } C \text{ — will also be a post-subsidy equilibrium. Further, when subsidies can be targeted, it is cheaper to make the middle class get the post-subsidy median income rather than the poor since } \mu^M \leq \mu^L. 

Result 3 shows that the total subsidy bill will be smaller under the targeted subsidy scheme vis-à-vis the uniform subsidy scheme whenever \((y^0 - y^M) \neq (\hat{y}^* - y^L)\). The targeted subsidy scheme utilizes the social multiplier effect: it gives just enough subsidy to the middle class for all its members to own even if the poor do not own, and then gives just enough subsidy to the poor for them to own given that the rich and the middle class own. Note that if \((y^0 - y^M) > (\hat{y}^* - y^L)\) (which is not precluded by our parameter restrictions), the subsidy is larger for the middle class than for the poor under the targeted scheme.

Finally, we study the issue of inefficient segregation. Consider the following symmetric outcome: \textit{Outcome D — where half the measures of the three income classes stay in each of the two communities, and in each community the poor rent and the others own.} Given \([R]\), if \(y^M > \max\{y^*(\mu^H, \bar{\rho}), y^0\}\), \(C\) is the only stable segregated equilibrium, and \(D\) is the only unstable symmetric equilibrium. In both outcomes, \(x_1 = x_2 = \mu^H + \mu^M\). As \(D\) involves relocating the homeowners in \(C\) equally between the two communities, if the net community quality function \(Q(\cdot)\) is strictly concave, then \(D\) is more efficient.

\textbf{Result 4.} Suppose that \([R]\) holds, and \(y^M > \max\{y^*(\mu^H, \bar{\rho}), y^0\}\). Consider the tax-subsidy scheme defined in the text. Set \(\bar{x} = (\mu^H + \mu^M)\). Then there exists a finite \(\lambda > \bar{x}\), \(D\) is the unique post-intervention stable equilibrium outcome.

\textit{Proof:} As the scheme involves no taxes or subsidies at \(D\), it is a post-intervention equilibrium. We now show that it is stable. The payoffs to the households at \(D\) are:
\[V^H(x) = u^H(y^H - \tau(x), x, \bar{\rho}) + \min\{c(y^H - \tau(x) - y^*(x, \bar{\rho})), S(x)\}, \] \[V^M(x) = u^H(y^M - \tau(x), x, \bar{\rho}) + c(y^M - \tau(x) - y^*(x, \bar{\rho}))\text{, and } V^L(x) = u^L(y^L + \sigma(x), x, \bar{\rho}).\]
Using the specifications of \(\tau(\cdot)\) and \(\sigma(\cdot)\), note that for any \(x\) in the neighborhood of \((\mu^H + \mu^M)\), \(V^H(x) \geq \max\{V^H_s(x), V^M_s(x)\}\) for \(\lambda > \max\{\mu^L S(x), (c\mu^L/[1+c\mu^L])[-y^*(x, \bar{\rho})]\}\). Then the arguments presented in the proof of Proposition 2 establish that post-intervention, \(D\) is stable. That there can be no other post-intervention stable equilibrium follows from the fact that in any community, if \(x >\) (resp., <) \((\mu^H + \mu^M)\), then for \(\lambda\) sufficiently large, the poorest owners (resp., the richest renters) will switch to renting (resp., owning) so as to go from paying a high tax to receiving a large subsidy.
References


Table 1. Local civic participation in the US: Homeowners compared to renters

<table>
<thead>
<tr>
<th>Source</th>
<th>Dimensions of civic participation</th>
<th>Effect of homeownership</th>
<th>Control variables</th>
</tr>
</thead>
</table>
| Cox 1982: Survey of 500 residents of Columbus, Ohio | Probability of neighborhood activism  
  • when facing a community problem  
  • in other cases | 0.39**  
  0.27** | Number of children in household |
| Rohe and Stegman 1994: Longitudinal study of 226 low-income homebuyers and renters in Baltimore | Number of community organizations that a resident household belongs to | 0.20** | Income, education, age, race, gender, marital status, children, dwelling type, satisfaction with neighborhood |
| Verba et al. 1995: Citizenship Participation Study of a cross-section of 15,000 adults in the US | Probability of local participation, e.g., voting in local elections, contacting local officials, protesting on local issues, attending local board meetings | 0.09** | Years in the community, income, education, race, gender, job level, parents’ education, free time, school-aged children |
| DiPasquale and Glaeser 1999: US General Social Survey | Probability of voting in local elections  
  Number of non-professional organizations that a household belongs to  
  Probability of knowing the identity of the school board head | 0.15**  
  0.25**  
  0.09** | Income, education, age, race, gender, marital status, children, city size |

**significant at 1% level; *significant at 5% level.

Table 2. Dissimilarity index of homeowner-renter segregation in the ten largest US MSAs, 1990

<table>
<thead>
<tr>
<th>Annual income</th>
<th>Non-blacks with children</th>
<th>Non-blacks, no children</th>
<th>Blacks with children</th>
<th>Blacks, no children</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt; $25,000</td>
<td>0.624</td>
<td>0.450</td>
<td>0.676</td>
<td>0.619</td>
</tr>
<tr>
<td>$25,000–50,000</td>
<td>0.423</td>
<td>0.351</td>
<td>0.576</td>
<td>0.618</td>
</tr>
<tr>
<td>$50,000–75,000</td>
<td>0.424</td>
<td>0.354</td>
<td>0.600</td>
<td>0.669</td>
</tr>
<tr>
<td>$75,000–100,000</td>
<td>0.570</td>
<td>0.414</td>
<td>0.799</td>
<td>0.824</td>
</tr>
<tr>
<td>&gt; $100,000</td>
<td>0.610</td>
<td>0.438</td>
<td>0.878</td>
<td>0.871</td>
</tr>
</tbody>
</table>

Data Source: 1990 US Census
Figure 1. The price of home equity in community \{x, \rho\}

\[
\begin{align*}
\beta^+ & = \rho + \delta p(n,x) \\
\beta & = \rho - \delta [p(e,x) - p(n,x)] \\
\alpha^* & \\
0 & \leq \alpha \leq 1
\end{align*}
\]

Discount = \( S(x) \)

Price of homeownership

Figure 2. Segregated outcomes in a two-community city

Outcome A         Outcome B         Outcome C

Community 1         Community 2   Community 1         Community 2   Community 1         Community 2

rich home-owners     middle class renters    rich home-owners     middle class renters    rich home-owners     middle class renters

middle class renters  poor renters         middle class renters  poor renters         middle class renters  poor renters