

# Geographical Disadvantage

## A Heckscher-Ohlin-von Thunen Model of International Specialization

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What effect does distance have on costs for economies at different locations? Exports and imports of final and intermediate goods bear transport costs that increase with distance. Production and trade depend on factor endowments and factor intensities as well as on distance and the transport intensities of different goods.

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## Summary findings

The combination of distance, poor infrastructure, and being landlocked by neighbors with poor infrastructure can make transport costs many times higher for some developing countries than for most others.

Drawing on two traditions of economic modeling — Heckscher-Ohlin trade theory and von Thunen's work on the "isolated state" — Venables and Limão analyze the trade and production patterns of countries located at varying distances from an economic center.

Predicting a country's production and trade pattern requires knowledge of the country's location, its factor endowment, and the factor intensities and transport intensities of goods.

Venables and Limão define transport intensity and show how location and transport intensity should be combined with factor abundance and factor intensity in determining trade flows. A theory based on only one set of those variables, such as factor abundance, will systematically make incorrect predictions.

They report that geography and endowments interact in such a way that the world divides up into economic zones with different trade patterns.

Countries close to the economic center may specialize in transport-intensive activities; countries further out become diversified, producing and sometimes trading more goods; countries still further out may become import-substituting (replacing some of their imports from the center with local production); in the extreme, regions become autarkic. More remote locations have lower real incomes.

Globalization changes the terms of trade, improving the welfare of regions further out from economic centers, though reducing the welfare of closer regions.

Where will a new activity, such as assembly of a new product, locate? Remote locations are disadvantaged if the product has high transport intensity (perhaps because of heavy requirements for intermediate inputs). But the costs of remoteness are already incorporated into the factor prices of those regions, which makes them more attractive. Which location is chosen depends, therefore, on how existing activities compare with the new activity in transport intensity and factor intensity.

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This paper — a product of Trade, Development Research Group — is part of a larger effort in the group to study the location of economic activity. Copies of the paper are available free from the World Bank, 1818 H Street, NW, Washington, DC 20433. Please contact Lili Tabada, room MC3-333, telephone 202-473-6896, fax 202-522-1159, email address [ltabada@worldbank.org](mailto:ltabada@worldbank.org). Policy Research Working Papers are also posted on the Web at [www.worldbank.org/research/workingpapers](http://www.worldbank.org/research/workingpapers). The authors may be contacted at [avenable@worldbank.org](mailto:avenable@worldbank.org) or [ng14@columbia.edu](mailto:ng14@columbia.edu). December 1999. (29 pages)

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**Geographical disadvantage:  
a Heckscher-Ohlin-von Thunen model of international specialisation.**

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## Non-technical summary:

'Geographical disadvantage: a Heckscher-Ohlin-von Thunen model of international specialization' A.J. Venables and N. Limao

Distance is a powerful explanatory variable in determining trade flows, as is demonstrated by countless applications of the gravity model, yet trade theory has remarkably little to say about its implications. How do distance and the associated transport costs determine not just the volume of trade, but also the patterns of trade, industrial structure, factor prices and income across countries? This question is particularly important for developing countries, some of which, even after trade liberalization, find participation in world trade impeded by transport costs and other real barriers to trade. The combination of distance, poor infrastructure, and perhaps also being landlocked by neighbours with poor infrastructure, can make transport costs many times higher for some developing countries than for most developed countries. For example, the costs of shipping a standard container from Baltimore to various West African destinations varies from \$3,000 (Cote D'Ivoire), through \$7,000 (Benin, Burkina Faso) to \$13,000 (Central African Republic). These costs have dramatic effects in choking off trade volumes -- estimates suggest that doubling transport costs can reduce trade flows by around 80%. Landlocked countries typically have average transport costs around 50% higher than otherwise similar coastal economies, giving trade volumes two-thirds lower (see Limao and Venables 1999).

The analysis of this paper is intended to be suggestive of the effects of these costs of distance on economies at different locations. Our approach is to take as given the existence of a centre of economic activity and show how the structure and income of countries varies as we move from locations close to this centre to locations which are more remote. The analysis is based on a combination of two traditions of economic modelling. One is the spatial economic analysis developed originally in von Thunen's celebrated work on the 'isolated state' (von Thunen (1826), Samuelson (1983)). Following this approach we assume the existence of a central location and a set of more remote locations. Locations at greater distance receive lower prices for their exports to the centre, and pay higher prices for any goods they import from the centre. The other tradition is the factor abundance approach of Heckscher-Ohlin trade theory, based on locations having fixed endowments of several types of factors of production and goods having different factor intensities. Thus, whereas von Thunen's regional analysis assumed that workers could move costlessly between locations, we interpret locations as countries and assume that workers (and other factors of production) are geographically immobile.

Our main results are, first, that the interaction of geography and endowments will generally cause the world to divide up into economic zones. Countries close to the centre may specialise in transport intensive activities. Moving further out, locations become diversified producing more goods and possibly (although not necessarily) trading more of them. Still further out, regions may become import substituting (replacing some of their imports from the centre with local production), and in the extreme, regions become autarkic. More remote locations have lower real incomes, although the incomes of particular factors of production may rise or fall, depending on the factor intensities of the products being produced and the factor endowments of the countries.

Second, predicting the production and trade pattern of a country requires that we know both its factor endowment and the factor intensities of goods, and its location and the transport intensities of goods; the analysis offers a precise definition of transport intensity and shows how location/ transport intensity should be combined with factor abundance/ factor intensity in determining trade flows. A theory based on just one of these sets of variables – eg factor abundance – will give systematically

incorrect predictions.

Third, we turn to a simple analysis of globalization, taken to be a reduction in transport costs on all activities. This is similar to moving all locations closer to the centre and tends to raise incomes. However, it also typically turns the terms of trade against non-central locations. On balance we find regions close to the centre experiencing welfare loss, and those further out gaining.

Finally, we address the question of where a new activity – such as assembly of a new product – might locate. Remote locations are disadvantaged if the product has high transport intensity (due perhaps to high imported intermediate input requirements). However, the costs of remoteness are already incorporated in the factor prices of these regions, increasing their attractiveness. The chosen location therefore depends on comparison of the transport intensity and factor intensity of the new activity with the intensities of existing activities.

## **1: Introduction:**

Distance is a powerful explanatory variable in determining trade flows, as is demonstrated by countless applications of the gravity model, yet trade theory has remarkably little to say about its implications. How do distance and the associated transport costs determine not just the volume of trade, but also the patterns of trade, industrial structure, factor prices and income across countries? This question is particularly important for developing countries, some of which, even after trade liberalization, find participation in world trade impeded by transport costs and other real barriers to trade. The combination of distance, poor infrastructure, and perhaps also being landlocked by neighbours with poor infrastructure, can make transport costs many times higher for some developing countries than for most developed countries.<sup>1</sup> These costs have dramatic effects in choking off trade volumes -- estimates suggest that doubling transport costs can reduce trade flows by around 80%. Landlocked countries typically have average transport costs around 50% higher than otherwise similar coastal economies, giving trade volumes two-thirds lower (see Limao and Venables 1999).

The analysis of this paper is intended to be suggestive of the effects of these costs of distance on economies at different locations. Our approach is to take as given the existence of a centre of economic activity and show how the structure and income of countries varies as we move from locations close to this centre to locations which are more remote. We see that the world divides up into zones with different production activities, factor prices, and real incomes. Some of these zones are export oriented, others import substituting, and some, in the extreme, may be autarkic.

The analysis is based on a combination of two traditions of economic modelling. One is the spatial economic analysis developed originally in von Thunen's celebrated work on the 'isolated

state' (von Thunen (1826), Samuelson (1983)). Following this approach we assume the existence of a central location and a set of more remote locations. Locations at greater distance receive lower prices for their exports to the centre, and pay higher prices for any goods they import from the centre. The other tradition is the factor abundance approach of Heckscher-Ohlin trade theory, based on locations having fixed endowments of several types of factors of production and goods having different factor intensities. Thus, whereas von Thunen's regional analysis assumed that workers could move costlessly between locations, we interpret locations as countries and assume that workers (and other factors of production) are geographically immobile. We also work with a more general production structure than is usual in these models, allowing commodities produced in the centre to be produced elsewhere, and adding intermediate goods in order to study the location of final assembly activities, important in many countries' development.

Combining these traditions gives outcomes determined by the interaction of two types of country characteristics with two types of commodity characteristics. The country characteristics are location and endowment of primary factors, and the commodity characteristics are transport intensity and factor intensity. We show how the interaction of these elements determines the pattern of trade and production. Thus, it is possible that all locations have the same production structures – but only if their endowments vary in a particular way, to cancel out changing locational effects. More generally, the world divides into economic zones, with both inter- and intra- zone differences in economic structures depending on location and endowments. Our results show a theory based on just one of these sets of interactions – for example, just factor abundance and factor intensity – will give systematically incorrect predictions.

We regard the model developed in the paper as a 'benchmark' model, showing how to

combine traditional comparative advantage and spatial economics, but ignoring many important considerations. In particular, the model is based entirely on constant returns to scale, perfect competition, and absence of market imperfections. We therefore abstract from the ‘linkages’ and cumulative causation processes studied in much of the new economic geography.<sup>2</sup>

The paper is organised as follows. In the following section we outline the model. Section 3 characterizes the equilibrium, first by looking at an illustrative example, and then by fuller analysis of the various zones of specialisation that form. Section 4 discusses comparative statics, both for their intrinsic interest, and to get a sense of the generality of the results of section 3. Section 5 looks at real income across space and illustrates how globalization -- taken to be a uniform reduction in all transport costs -- may benefit some locations and harm others. Section 6 looks at the attractiveness of different locations for production of a newly tradeable activity, and section 7 concludes.

## **2. The model**

Our model will, in the tradition of von Thunen, take as given a central location in which there is a concentration of certain economic activities. The central location has the defining properties that (a) there is one good (or composite of goods) that is exported by the central location, (b) the central location imports all other tradeable goods,<sup>3</sup> and (c) all other locations can be arranged on a line going through the centre. Assumptions (a) and (b) are restrictive, but not out of line with the context of this paper. For example, we can think of the central location as the established manufacturing regions, and take these to be exporters of a range of high technology manufactures (or services). We allow these goods to be used in other locations both for final consumption and as intermediates in production. We do not model the reason for the centre’s trade pattern although this

could easily be done, by giving the centre the appropriate factor endowment, or some Ricardian advantage, or by modelling agglomeration forces binding production of certain goods to the centre. Assumption (c) restricts the geography of the world to be one dimensional. We doubt that the generalisation to two dimensions would change qualitative results.

Locations away from the centre are endowed with two immobile factors of production, and we have to determine the mix of goods that each produces and trades. All goods are subject to trade costs which depend on the distance shipped, so arbitrage generates price functions over the space; these price functions have to be lined up with production costs in locations where a good is produced. We shall see that this determines factor prices in all locations and gives rise to zones in which different mixes of goods are produced.

Turning to a more formal model description, let us assume that there are three tradable goods, which will be subscripted 0, 1 and 2. The geographical space is the real line, points on which are labelled  $z$  so, for example,  $p_i(z)$  and  $x_i(z)$  denote the price and production of good  $i$  at location  $z$ . We take point 0 as the central location, and look only at points to the right of 0 ( $z > 0$ ), since the concentration of activities at 0 means that there is no interaction between economies on either side of this point.

Goods are subject to iceberg trade costs, so to deliver one unit of good  $i$  from location  $r$  to location  $z$ ,  $\tau_i(r, z) \geq 1$  units have to be shipped. We assume that these costs are exponential, so  $\tau_i(r, z) = \exp[t_i|r - z|]$ . We are able often to focus on transport costs between the centre and location  $z$ , and write  $\tau_i(z) \equiv \tau_i(0, z) = \exp[t_i z]$ .

The central location has a predetermined pattern of trade, exporting good 0 and importing goods 1 and 2. The price of  $x_0$  at location 0 is unity, so the border price at location  $z$  is simply  $\tau_0(z)$ .

Income at the central location we assume to be fixed in terms of the good 0 (an assumption that can easily be given micro-foundations). The centre's imports of the other two goods, denoted  $c_i(0)$ , are given by import demand functions,

$$c_1(0) = c_1(p_1(0), p_2(0)), \quad c_2(0) = c_2(p_1(0), p_2(0)), \quad (1)$$

which we assume to be strictly positive.

Other locations,  $z > 0$ , are endowed with quantities of two factors, labour and capital; we denote these  $L(z)$ ,  $K(z)$ , and assume that they are zero beyond some value of  $z$  which defines the edge of the economy.<sup>4</sup> Factor prices are  $w(z)$  and  $r(z)$ , creating income levels

$$y(z) = w(z)L(z) + r(z)K(z). \quad (2)$$

Consumers at each location consume all three goods. Their utility is  $u(z)$  and their preferences are described by a homothetic expenditure function, so the equality of income to expenditure is

$$y(z) = e(p_0(z), p_1(z), p_2(z))u(z). \quad (3)$$

Each of these locations can produce the goods  $x_0$ ,  $x_1$  and  $x_2$ , using primary factors and possibly also good  $x_0$  as an intermediate; unit costs are expressed as  $b_i(w(z), r(z), p_0(z))$ ,  $i = 0, 1, 2$ . In any location where good  $i$  is produced price equals unit cost, so

$$p_i(z) \leq b_i(w(z), r(z), p_0(z)), \quad x_i(z) \geq 0, \quad \text{complementary slack}, \quad i = 0, 1, 2. \quad (4)$$

Factor market clearing at each location is given by

$$\begin{aligned}
L(z) &= x_0(z) \frac{\partial b_0(w, r, p_0)}{\partial w} + x_1(z) \frac{\partial b_1(w, r, p_0)}{\partial w} + x_2(z) \frac{\partial b_2(w, r, p_0)}{\partial w} \\
K(z) &= x_0(z) \frac{\partial b_0(w, r, p_0)}{\partial r} + x_1(z) \frac{\partial b_1(w, r, p_0)}{\partial r} + x_2(z) \frac{\partial b_2(w, r, p_0)}{\partial r}.
\end{aligned} \tag{5}$$

It remains to determine the price functions,  $p_i(z)$ , and these are illustrated on figure 1. First consider  $p_0(z)$ . Since this is numeraire,  $p_0(0) = 1$ , and as we move away from  $z = 0$  the price function increases exponentially, deterring imports of the good. We define  $z_0^*$  as the first location across which there is no outwards flow of good 0. (Or equivalently, there is no net import demand for good 0 coming from the right of  $z_0^*$ ; such a point may or may not exist). To the left of  $z_0^*$  the price is set by imports from the centre, so  $p_0(z) = \tau_0(z)$ . Locations beyond  $z_0^*$  are ‘disconnected’ from the centre, and have  $p_0(z) \leq \tau_0(z)$  (if this inequality were reversed, it would be profitable to supply them from the centre). We assume that all such locations are self-sufficient in good 0, so have price  $p_0^a(z)$  implicitly defined by the equality of local supply and demand (coming from consumption and from intermediate demand),

$$\begin{aligned}
p_0^a(z) &= b_0(w(z), r(z), p_0^a(z)), \quad \text{with} \\
x_0(z) &= \frac{\partial e(p_0^a(z), p_1(z), p_2(z))}{\partial p_0} u(z) + \sum_i \frac{\partial b_i}{\partial p_0} x_i(z)
\end{aligned} \tag{6}$$

This is illustrated by the wiggly line  $p_0^a(z)$ . What underlying assumption supports self sufficiency of these regions? A sufficient condition is that  $\tau_0(r, r+s)p_0^a(r) > p_0^a(r+s)$  for all  $r$ ,  $r+s > z_0^*$ . This says that if locations  $r$  and  $r+s$  are self sufficient, it is not worthwhile shipping between them. It will be satisfied providing  $p_0^a(z)$  does not vary too much between locations, which is in turn

ensured if relative endowments do not vary too much.<sup>5</sup> We make this assumption from now on.

Summarizing, we have price function  $p_0(z)$  given by:

$$\begin{aligned} \text{For } z < z_0^*, \quad p_0(z) &= \tau_0(z). \\ \text{For } z = z_0^*, \quad p_0(z) &= \tau_0(z) = p_0^a(z). \\ \text{For } z > z_0^*, \quad p_0(z) &= p_0^a(z) \leq \tau_0(z). \end{aligned} \tag{7}$$

Notice that it may not be the case that all locations in  $(0, z_0^*)$  import good 0 from the centre. For example, some locations in  $(0, z_0^*)$  could export good 0, but providing there is still an outwards flow of the good through these locations, they will have price given by  $p_0(z) = \tau_0(z)$ .

The determination of the price functions for the other two goods,  $p_1(z)$  and  $p_2(z)$ , has two components -- the level of the functions, as determined by central prices  $p_1(0)$  and  $p_2(0)$ , and their shapes away from the centre. The shapes depend on transport costs, in a manner analogous to  $p_0(z)$ , although since these products are shipped *to* the centre, the function has negative gradient, as illustrated on figure 1. We define  $z_1^*$  and  $z_2^*$  as the furthest locations across which there is no flow of good 1 (respectively 2) to the centre. To the left of these points prices are set by central prices net of transport costs, and to the right we assume that locations are self-sufficient. We therefore have, for  $i = 1, 2$ :

$$\begin{aligned} \text{For } z < z_i^*, \quad p_i(z) &= p_i(0)/\tau_i(z). \\ \text{For } z = z_i^*, \quad p_i(z) &= p_i(0)/\tau_i(z) = p_i^a(z). \\ \text{For } z > z_i^*, \quad p_i(z) &= p_i^a(z) \geq p_i(0)/\tau_i(z). \end{aligned} \tag{8}$$

Finally, we must find the level of the price functions by finding  $p_1(0)$  and  $p_2(0)$ . This is determined

by overall supply and demand for each good, which takes the form,

$$\begin{aligned} \int_0^\infty x_i(z) dz &= c_i(0) + \int_0^\infty \frac{\partial e(p_0(z), p_1(z), p_2(z))}{\partial p_i(z)} u(z) dz + T_i \\ T_i &\equiv \int_0^\infty \left[ x_i(z) - \frac{\partial e(p_0(z), p_1(z), p_2(z))}{\partial p_i(z)} u(z) \right] (\tau_i(z) - 1) dz \end{aligned} \quad (9)$$

where demand consists of consumption demand at the centre, at all other points, and also quantities of the good used up in shipping,  $T_i$ , as given in the second equation.

### 3. Zones of specialisation

We are now in a position to investigate characteristics of the equilibrium, and we start by looking at the pattern of specialisation across countries. This is most easily done if we first illustrate the equilibrium, and then investigate its properties analytically.

**3.1: Illustration:** We start by illustrating an example constructed with good 1 having a higher transport intensity than good 2 -- we offer a precise definition of transport intensity later. In the example endowments are assumed to be the same in all locations (further details of the example are given in the appendix). Figure 2 gives the gross output of industries across locations (measured on the horizontal axis), figure 3 gives the exports and imports of each location, and figure 4 the cumulated trade flows from outlying regions to the centre. Figure 5 gives the real income and factor

prices at each location. The figures show how the world economy divides up into zones, and we discuss each of those zones in turn. Fuller description and analysis follows in the next sub-section.

At low values of  $z$ , i.e. locations close to the centre, there is a region which we label zone I. Locations in this zone specialise in good 1, the relatively transport intensive good, exporting this good and importing goods 0 and 2.

Adjacent is zone II, defined as the set of locations producing goods 1 and 2 and exporting good 1. As we move outwards across zone II production of 1 falls and production of 2 increases, with locations beyond some point becoming exporters of good 2 (see figure 3). The shift from good 1 to good 2 production occurs because of the lower transport intensity of good 2. The fact that there is more than one immobile factor means that – unlike in von Thunen – there is not complete specialisation of regions, but instead this area of overlap within which both activities are active. The two goods have different factor intensities -- we label factors such that good 2 is capital intensive -- and this gives the diverging factor prices illustrated in figure 5.

Moving further out again, we enter zone III, in which it is not profitable to export good 1. This occurs as we pass point  $z_1^*$ , so that locations become self sufficient in good 1, while continuing to export good 2.

Zone IV is one of import substitution – good 0 has become so expensive that it is profitable to produce it locally. Within this zone each location imports good 0 and exports good 2, but in smaller quantities as we move further out. In our example good 0 is relatively labour intensive, and this brings the change in direction in relative factor prices (figure 5). Eventually, in zone V, there is autarky. The dividing line between zones IV and V is location  $z_0^* = z_2^*$ ; the two points must coincide, because of payments balance.

While figure 3 gives the trade flows of each location, it is also instructive to look at the flow of goods across locations, and this is given in figure 4, in which the curves for goods 1 and 2 are cumulative exports from outer locations towards the centre, and for good 0, cumulative imports of outer locations from the centre. We see that  $z_1^*$  is the first point at which there is no flow of good 1 to the centre; since all locations to the left of this point are net exporters of good 1, the flow increases steadily as we approach the centre. For goods 0 and 2, flows go to zero on the boundary between zones IV and V. Notice that for good 2 the cumulative flow curve increases steadily until some point in zone II at which production of good 2 drops below consumption. The curve then declines, until its intercept with the vertical axis gives the quantity of good 2 delivered to the centre.

**3.2: Analysis:** The example raises a number of issues which we now address analytically, zone by zone.

*Zone I:* Let us initially take as given the existence of a zone of specialisation close to the centre, labelling goods such that good 1 is produced in the zone. Production is characterised by

$$p_1(0) = \tau_1(z)b_1(w(z), r(z), \tau_0(z)), \quad \varphi(z) \equiv p_2(0) - \tau_2(z)b_2(w(z), r(z), \tau_0(z)) < 0. \quad (10)$$

where the first equation says that good 1's marginal cost of supply (inclusive of transport costs) equals the price in the centre, and the second defines  $\varphi(z)$  as the amount by which the central price of good 2 exceeds or falls short of industry 2 cost (including the cost of shipping) at location  $z$ ; since it is not profitable to produce this good in zone I, we have  $\varphi(z) < 0$ . Factor market clearing at each location in zone I implies

$$\frac{\partial b_1 / \partial w}{\partial b_1 / \partial r} = \frac{L(z)}{K(z)}. \quad (11)$$

What happens as we move outwards from the centre, while staying within zone I? We find the answer by totally differentiating (10) and (11). As we do this (and subsequent exercises) we denote proportionate changes in variables with respect to a change in  $z$  by  $\hat{\cdot}$ , and the shares of labor, capital, and intermediates in production in industry  $i$  by  $\alpha_i, \beta_i, \gamma_i$  respectively ( $\alpha_i + \beta_i + \gamma_i = 1$ ). The derivative of (11) is, from the definition of the elasticity of substitution<sup>6</sup>,  $\sigma_i$ ,  $(\hat{L} - \hat{K}) = \sigma_1(\hat{r} - \hat{w})$ . Using this in the total derivative of industry 1's break even condition (equation (10)) gives the following expressions for the changes in factor prices:

$$\begin{aligned}\hat{w} &= \frac{(\hat{K} - \hat{L})\beta_1/\sigma_1 - (t_1 + \gamma_1 t_0)}{1 - \gamma_1} \\ \hat{r} &= \frac{(\hat{L} - \hat{K})\alpha_1/\sigma_1 - (t_1 + \gamma_1 t_0)}{1 - \gamma_1}.\end{aligned} \quad (12)$$

These say that changes in factor prices are driven by two components. One is transport costs on good 1 and on the intermediate good 0, causing both factor prices to fall equi-proportionately. The other is changing relative factor endowments, as measured by  $\hat{L} - \hat{K}$ . In figure 5 we assumed that  $\hat{L} = \hat{K}$ , so  $w$  and  $r$  both decline at the same rate. If, however,  $\hat{L} - \hat{K} \neq 0$ , then one of the factor prices may increase if its endowment becomes sufficiently scarce at more distant locations.

Movements in factor prices hold industry 1 at break-even, and also change the potential profitability of industry 2,  $\phi(z)$ . The movement of  $\phi(z)$  within zone I is

$$\frac{\hat{\phi}}{1 - \gamma_2} = \left( \frac{t_1 + \gamma_1 t_0}{1 - \gamma_1} - \frac{t_2 + \gamma_2 t_0}{1 - \gamma_2} \right) + (\hat{K} - \hat{L}) \left( \frac{\beta_2}{(1 - \gamma_2)\sigma_2} - \frac{\beta_1}{(1 - \gamma_1)\sigma_1} \right) \quad (13)$$

(derived by totally differentiating the expression in (10) and using (12)). Industry 2 is moving towards profitability if  $\hat{\phi} > 0$ . Suppose first that relative endowments are uniform across space, so  $\hat{K} - \hat{L} = 0$ . Good 2 is then moving towards profitability if the first term is positive, and we shall say that good 2 is *relatively transport unintensive* (good 1 is *relatively transport intensive*) if this holds, i.e.

$$\text{good 1 transport intensive: } \frac{t_1 + \gamma_1 t_0}{1 - \gamma_1} > \frac{t_2 + \gamma_2 t_0}{1 - \gamma_2}. \quad (14)$$

These expressions give the proportionate change in transport costs -- on sales and on imported inputs -- from an increase in distance, per unit value added (since  $1 - \gamma_i$  is the share of primary factors in costs). We see immediately that good 1 is more transport intensive the larger is  $t_1$  and the larger is the share of imported inputs in its costs,  $\gamma_1$ .

Two comments are in order. First, the condition tells us that it is not transport costs per unit value output that matter in determining location. Instead it is transport costs per unit value added, since this is the criterion which minimises resource cost per unit sales, as we know from the literature on effective protection. Second, since transport costs are exponential in distance the terms  $t_i$  are constants, and if technologies are Cobb-Douglas, so too are the  $\gamma_i$ . More generally however, we cannot rule out ‘transport intensity reversals’.

We can see from equation (13) that if relative endowments are uniform, then the good

produced in zone I must be that which is more transport intensive. If not, equation (13) would be negative,  $\phi(z)$  would be decreasing, and good 2 would never produced, which cannot be an equilibrium. What we have shown then is that the intuition that transport intensive goods are produced close to the centre is formalised in the first term of equation (13) and the definition of transport intensity.

What if  $\hat{K} - \hat{L} \neq 0$ ? The profitability of good 2 in different locations then depends both on its relative transport intensity and on the changing relative factor abundance of these locations. This is most readily interpreted if the elasticities of substitution in the two industries are the same, in which case the second term in (13) is proportionate to  $(\hat{K} - \hat{L})(\alpha_1\beta_2 - \alpha_2\beta_1)$ . If regions become more capital abundant and good 2 is capital intensive (so  $\alpha_1\beta_2 - \alpha_2\beta_1 > 0$ ) then this is positive, promoting the profitability of industry 2. More generally, equation (13) tells us how to combine the relative transport intensities of industries with their comparative advantage due to factor intensity differences. Transport costs are more important relative to factor endowments the greater is the difference in factor intensities between the two products, and the higher are the elasticities of substitution between primary factors.

*Zone II:* In zone II both goods 1 and 2 are produced, and the production mix changes as we move to more distant locations. Zero profit conditions for the two industries are,

$$\begin{aligned} p_1(0) &= \tau_1(z)b_1(w(z), r(z), \tau_0(z)), \\ p_2(0) &= \tau_2(z)b_2(w(z), r(z), \tau_0(z)), \end{aligned} \tag{15}$$

and totally differentiating these equations we derive the following expression for the change in

relative factor prices,

$$\hat{w} - \hat{r} = \frac{(1 - \gamma_1)(t_2 + \gamma_2 t_0) - (1 - \gamma_2)(t_1 + \gamma_1 t_0)}{\alpha_1 \beta_2 - \alpha_2 \beta_1}. \quad (16)$$

The denominator of expression (16) gives the relative capital-labour ratios of the two industries, and is positive if industry 1 is labour intensive. The numerator gives the correct way of measuring the effects of changing location as transmitted through transport costs, and is the expression for relative transport intensity that we saw in equation (13). If good 1 is transport intensive this is negative and *w/r* (the relative price of the factor intensive in good 1) decreases at more distant locations. This causes both industries to become more labour intensive, so full employment of factors requires that industry 1 – the labour intensive sector – shrinks and industry 2 expands, giving the changing industry production levels that we see in zone II of figure 2.

It is worth noting that each location in zone II has the characteristics of a Heckscher-Ohlin economy. Equation (16) says that factor prices change *only* because of transport costs, and are independent of factor endowments and preferences (termed ‘factor price insensitivity’ by Leamer and Levinsohn 1995). The reason is of course that the number of goods which are both produced and traded (two) is the same as the number of factors. As a corollary, we know how any variations in endowments affects production – just through Rybczynski effects.

The factor price changes as we move across zone II are of interest in their own right.

Expressing each separately we have,

$$\hat{w} = \frac{\beta_1(t_2 + \gamma_2 t_0) - \beta_2(t_1 + \gamma_1 t_0)}{\alpha_1\beta_2 - \alpha_2\beta_1} \quad (17)$$

$$\hat{r} = \frac{\alpha_2(t_1 + \gamma_1 t_0) - \alpha_1(t_2 + \gamma_2 t_0)}{\alpha_1\beta_2 - \alpha_2\beta_1}$$

Intuition on these comes from Stolper-Samuelson, although the expressions are complicated by the fact that both output prices and the intermediate input price are changing. If only good 1 is subject to transport costs, we have the usual Stolper-Samuelson effects; as we move away from the centre  $r$  increases and  $w$  falls, and this fall is larger than the price fall (since  $\beta_2 > (\alpha_1\beta_2 - \alpha_2\beta_1)$ ). More generally, it is possible that both factor prices fall, although not that both rise. These are nominal changes; the real changes (deflated by the unit expenditure function) are shown in figure 5, and we see Stolper-Samuelson effects in operation.

*Zone III:* Locations in zone III export good 2, are self sufficient in good 1, and import all their good 0. The price - cost equations are

$$p_2(0) = \tau_2(z)b_2(w(z), r(z), \tau_0(z)),$$

$$p_1^a(z) = b_1(w(z), r(z), \tau_0(z)) > p_1(0)/\tau_1(z), \quad (18)$$

$$\tau_0(z) < b_0(w(z), r(z), \tau_0(z)).$$

The first equation says that, for good 2, price is set by sales to the centre; the second says that exports of good 1 to the centre are not profitable, so the price is the self-sufficiency price; the third says that it is cheaper to import good 0 than to produce it domestically. Notice that economies in zone III are not 'Heckscher-Ohlin like': only one good (good 2) is both produced and traded, and as

a consequence factor prices depend on local endowments and local preferences (since these enter the self-sufficiency price,  $p_i^a(z)$ ).

Although the inequality in the second equation (18) implies that it is not worth any zone III location selling good 1 to the centre, we must ensure that it is not profitable to export to some other location -- eg a neighbouring point in zone III. Location  $z$  cannot profitably export to location  $s+z$  if cost differences between the locations are less than transport costs on the product, i.e., if  $p_1(z) < t_1(s)p_1(s+z)$ . As discussed earlier, this condition will be satisfied providing differences in factor endowments between the locations are not too large.

*Zone IV:* Import substitution commences in this region, with locations producing all three goods. Since both good 0 and good 2 are traded with the centre, prices satisfy,

$$\begin{aligned} p_0(z) &= \tau_0(z) = b_0(w(z), r(z), \tau_0(z)), \\ p_2(0) &= \tau_2(z)b_2(w(z), r(z), \tau_0(z)). \end{aligned} \tag{19}$$

Good 1 is produced just for local sale, as in (18). Equations (19) determine factor prices, and totally differentiating them we derive

$$\begin{aligned} \hat{w} &= \frac{\beta_2(1 - \gamma_0)t_0 + \beta_0(t_2 + \gamma_2 t_0)}{\alpha_0\beta_2 - \alpha_2\beta_0}, \\ \hat{r} &= - \left[ \frac{\alpha_2(1 - \gamma_0)t_0 + \alpha_0(t_2 + \gamma_2 t_0)}{\alpha_0\beta_2 - \alpha_2\beta_0} \right], \\ \hat{w} - \hat{r} &= \frac{(1 - \gamma_0)(t_0 + t_2)}{\alpha_0\beta_2 - \alpha_2\beta_0}. \end{aligned} \tag{20}$$

Like zone II, these economies have factor prices independent of endowments and preferences. The technical coefficients and transport intensities that determine these prices are now those of industries 2 and 0, and the equations are different in form from those that apply in zone II (equations 18) because good 0 is an input to production. We see that  $w$  and  $r$  must move in opposite directions, with  $w$  increasing if good 0 is labour intensive compared to good 2.

*Zone V:* In autarky prices are all set by local supply and demand, with prices of goods 1 and 2 exceeding the border prices ( $p_i(z) = p_i^a(z) > p_i(0)/\tau_i(z)$  for  $i = 1, 2$ ) and the price of good 0 less than the border price ( $p_0(z) = p_0^a(z) < \tau_0(z)$ ).

#### 4. Comparative statics

Figures 2 - 5 do not illustrate the only possible configuration of regions. Obviously, it is possible to select the factor endowment of a particular point in a way such that the point produces, say, just good 1. In general, how does the structure of these zones depend on parameters of the model?

**4.1: Demand:** The sizes of the zones depend on overall supply and demand for the goods. For example, consider the effects of reducing the centre's demand for good 1. This will shrink zone I and, if demand is small enough, cause it to disappear, so zone II then runs up to the centre. Even so, the general point remains that transport intensive industries will produce close to the centre, unless transport intensity effects are overturned by variations in endowments.

**4.2: Transport costs:** In section 5 we investigate the effects of reductions in transport costs that affect all sectors. What about differences in transport costs between industries? The relative transport intensities of industries 1 and 2 determine where each is located, as previously discussed. The more similar are the transport intensities of industries 1 and 2, then the wider will be the zones in which both are produced. What about good 0? If transport costs on this good are very low then import substitution zones (IV and V) will not occur, while if they are sufficiently high zone III will not exist (domestic production of good 0 will start in the region where both goods 1 and 2 are exported).

**4.3: Factor intensities:** How do our results depend on the factor intensities of the different industries? The relative intensities of goods 1 and 2 is simply a matter of labelling (we have made 1 the more labor intensive). The more similar the factor intensities of the two goods, the sharper are the changes in production patterns across space (recall that if there is a single factor then there are no areas of overlap) and the smaller the changes in relative factor prices. Good 0 is, in the example illustrated in the figures, made labour intensive relative to both goods. Changing this would not change the zones of specialisation, but would alter the factor price story illustrated on figure 5; if good 0 were the most capital intensive good then, instead of converging, relative factor prices would diverge further as we move out to zones IV and V.

**4.4: Factor endowments:** We saw in section 3.2 that the production mix within zones depends on factor endowments, and so too can the overall arrangement of the zones. Evidently, patterns of endowment can be constructed to give different patterns of specialisation. A few intuitive points

can be made. For example, suppose that more remote locations are more abundant in labour, the factor used intensively in the transport intensive sector; then this will tend to shift the zone II/III boundary further to the right, since the more labour intensive good (good 1) will continue to be produced at the more labour intensive locations. Alternatively, we could ask, what pattern of factor endowments holds the relative exports of goods 1 and 2 the same for all locations? If both goods 1 and 2 are traded, then the configuration is as described in zone II. If the transport intensive sector is labour intensive, then the  $w/r$  ratio falls at further locations, (as in figure 5), making production in both sectors more labour intensive. To hold relative trade levels constant, further locations must therefore have more labour intensive endowments.<sup>7</sup> The main point to note is that in this case, although factor endowments vary across space, the pattern of trade does not – the differential transport intensities overturn Heckscher-Ohlin predictions about the pattern of trade.

## 5. Transport costs and real incomes

Figure 5 illustrates that real income falls steadily the further are locations away from the centre, up to the point at which they are autarkic. For given endowments, the change in real income is – to a first order approximation obtained by differentiating (3) – simply the change in transport costs times the value of trade,

$$-\hat{u} = \left( \frac{p_0(z)m_0(z)}{y(z)} \right) t_0 - \left( \frac{p_1(z)m_1(z)}{y(z)} \right) t_1 - \left( \frac{p_2(z)m_2(z)}{y(z)} \right) t_2 \quad (21)$$

$$\geq 0 \quad \leq 0 \quad ?$$

where  $m_i(z)$  is net imports of good  $i$  at location  $z$ , so the bracketed terms are import and export

shares in income. Imports are non-negative for good 0, non-positive for good 1 (exported or self-sufficient at all locations), and for good 2, switch from being positive to negative in zone II. The main point to note from this is that the real income loss arises on all elements of the gross trade flows – on imports and exports, and on intermediates as well as final goods; these might be large relative to value added,  $y(z)$ , the denominators in this expression.

What happens if transport costs in all sectors increase or decrease? The simplest experiment is to change all transport costs equi-proportionately while holding central prices,  $p_i(0)$ , constant. An increase in transport costs is then just a stretching of the horizontal axis of figures 2 - 5, and a decrease a compression (zones all move further from the centre), meaning that the zones further out might cease to exist. This says simply that if transport costs are low enough then even the furthest zones will trade (zone V does not exist), may not be import substituting (zone IV does not exist), and may perhaps continue to export good 1 (zone III does not exist). Holding prices constant, all locations away from the centre experience a real income increase as a consequence of the lower transport costs.

As transport costs and the location of production change, so do the quantities supplied to, and demanded from, the centre, and this will generally turn the terms of trade against non-central locations. The effects of a 10% reduction in transport costs on real incomes and factor prices are illustrated in figure 6, where light lines give the initial position (identical to figure 5) and bold ones the new position. The real income loss from the terms of trade changes hits all locations that trade, while the gain from the lower transport costs is of greater value to more remote locations. This creates the pattern we see, of locations relatively close to the centre experiencing real income loss and more remote locations gaining – unless they remain self-sufficient hence unaffected.

## 6. Where are new activities located?

It is sometimes suggested that regions with high transport costs are disadvantaged as locations for assembly production, or for other sorts of activity that can now be moved from their traditional locations. Clearly, there is some truth in this, in so far as such activities may be transport intensive, requiring both high volumes of imported inputs and the export of a high proportion of their output. However, simple statements of the argument ignore the fact that distant locations already bear a transport cost disadvantage on their exports, and that this is already incorporated in their factor prices. To find the location where some new activity will become established, we must therefore compare both its transport intensity and its factor intensity with those of existing activities.

To analyse this, let us take the equilibrium described so far, and suppose that a new good (good 3) can now be produced at any location, and that at least part of its output will be shipped to the centre. It will be produced in the location that offers the lowest unit cost, including transport, i.e. the  $z$  that minimizes  $\tau_3(z)b_3(w(z), r(z), \tau_0(z))$ . Using our previous example, we can find, for different values of good 3's transport intensity and factor intensity, the location where this is minimised.<sup>8</sup>

Results are plotted on figure 7. The horizontal axis is the labour-capital ratio for good 3, and the two points marked are the labour-capital ratios for goods 1 and 2. The vertical axis is the transport intensity of good 3,  $(t_3 + \gamma_3 t_0)/(1 - \gamma_3)$ , and the points marked are the transport intensities of goods 1 and 2. Regions of the figure are labelled according to the zone in which production of good 3 is cheapest.

The figure is quite complex, but we see that the location of good 3 depends on transport

costs and factor intensities in intuitive ways. It will locate closer to the centre, the higher its transport intensity,  $(t_3 + \gamma_3 t_0)/(1 - \gamma_3)$ . When it is more transport intensive than goods 1 and 2 it will locate in zone I, adjacent to the centre (0/I), unless it is also more labour intensive than both of them – in which case it may go to the location at the far edge of zone II (the zone II/III boundary), where the wage is lowest relative to the capital rental rate (see figure 5). Conversely, if good 3 is less transport intensive than goods 1 and 2 then it will locate in (or on the edge of) the import substituting or autarky regions, unless it is very much less labour intensive, in which case it may be drawn to the far edge of zone I (zone I/II boundary), where  $r/w$  is low. In the intermediate range of transport intensity we see that the cost minimising location could be in zones I, II or III, and is further out the more labour intensive is good 3; once again, this follows from the relative values of  $w/r$  in figure 5.

The general point is then that location of new investment depends on both its transport intensity and its factor intensity, each relative to those of existing activities. However, since the pattern of location of existing activities is itself endogenous and varying across space, the details are inevitably complex.

## 7. Concluding comments

Transport costs vary widely across goods and across locations, typically reaching peaks for landlocked developing countries (see Limao and Venables (1999)). A theory of trade that ignores these costs will yield systematically incorrect predictions about trade patterns, industrial structure, and factor incomes. This paper shows how to combine transport costs with a standard factor abundance trade model. There are several main findings.

First, although the model has an essentially Heckscher-Ohlin structure (each location has primary factors that can be used in any of the constant returns industries), factor endowments and factor intensities are not sufficient to predict the structure of production or pattern of trade. This also depends on the location of the country – in particular its remoteness from the economic centre – and on the transport intensity of goods. A precise definition of transport intensity is given, depending on the costs of shipping both final output and the intermediates used in production.

Second, remoteness reduces real income, other things being equal. Its effects on the prices of different factors is more complex, depending on the interactions between transport intensity and factor intensity; it is possible that the return to particular factors may peak at locations away from the centre. Transport costs are the reason for the real income penalty suffered by remote regions, but reducing transport costs will not necessarily benefit all regions. Induced supply responses will cause terms of trade changes, so typically a reduction in transport costs will increase real income in relatively remote regions, but may reduce it in less distant regions.

Finally, we consider the location of a newly tradable activity. Remote regions need not be a poor location for the activity, since their remoteness is already reflected in their factor prices. Choice of location depends on both the factor intensity and the transport intensity of the new activity, compared to these intensities in existing activities.

## Appendix:

Figures 1 - 4 are constructed with Cobb-Douglas preferences with expenditures equally divided between the three goods. Technologies are Cobb-Douglas with input share coefficients:

	Labour	Capital	Good 0
Good 0	0.62	0.38	0
Good 1	0.435	0.315	0.25
Good 2	0.336	0.464	0.2
Good 3	0.33	0.42	0.25

Functions  $t_i(z)$  are exponential,  $t_i(z) = \exp(t_i z)$ , with  $t_0 = 0.25$ ,  $t_1 = 0.3$ ,  $t_2 = 0.2$ ,  $t_3 = 0.2$ . This gives transport intensities,

$$\frac{t_1 + \gamma_1 t_0}{1 - \gamma_1} = 0.483, \quad \frac{t_2 + \gamma_2 t_0}{1 - \gamma_2} = 0.312, \quad \frac{t_3 + \gamma_3 t_0}{1 - \gamma_3} = 0.35. \quad (22)$$

The economy is one unit distance from centre to edge, so to deliver one unit of good 0 from centre to edge requires that 1.284 (=exp(0.25)) units be shipped; for goods 1 and 2 the corresponding numbers are 1.35 and 1.22.

In section 5 transport costs are reduced to 90% of the levels given above. Terms of trade change calculations are abased on the centre having import demand functions with elasticity of 2.

## Endnotes:

1. The costs of shipping a standard container from Baltimore to various West African destinations varies from \$3,000 (Cote D'Ivoire), through \$7,000 (Benin, Burkina Faso) to \$13,000 (Central African Republic). Estimates of transport costs and of the elasticity of trade with respect to transport costs come from Limao and Venables (1999).

2. See Fujita, Krugman and Venables (1999) for development of these alternative models.
3. All goods can be produced at all locations, so these assumptions refer to trades not production
4. Of course, the factors capital and labour are just conventional labels. They can equally well be thought of as two types of labour or labour and land.
5. This statement can be made precise by mapping out how prices change with endowments. It is complex, and no particular insight is gained from so doing.
6. Assuming capital and labour are separable from the intermediate input.
7. This case corresponds to all locations that trade being in zone II. Factor prices then move according to equation (16), from which it is straightforward to calculate endowments that hold relative exports of goods 1 and 2 constant.
8. Our experiment is to ask where a ‘small’ amount of good 3 production will locate, given the initial equilibrium prices. We do not allow production of good 3 to change factor prices.

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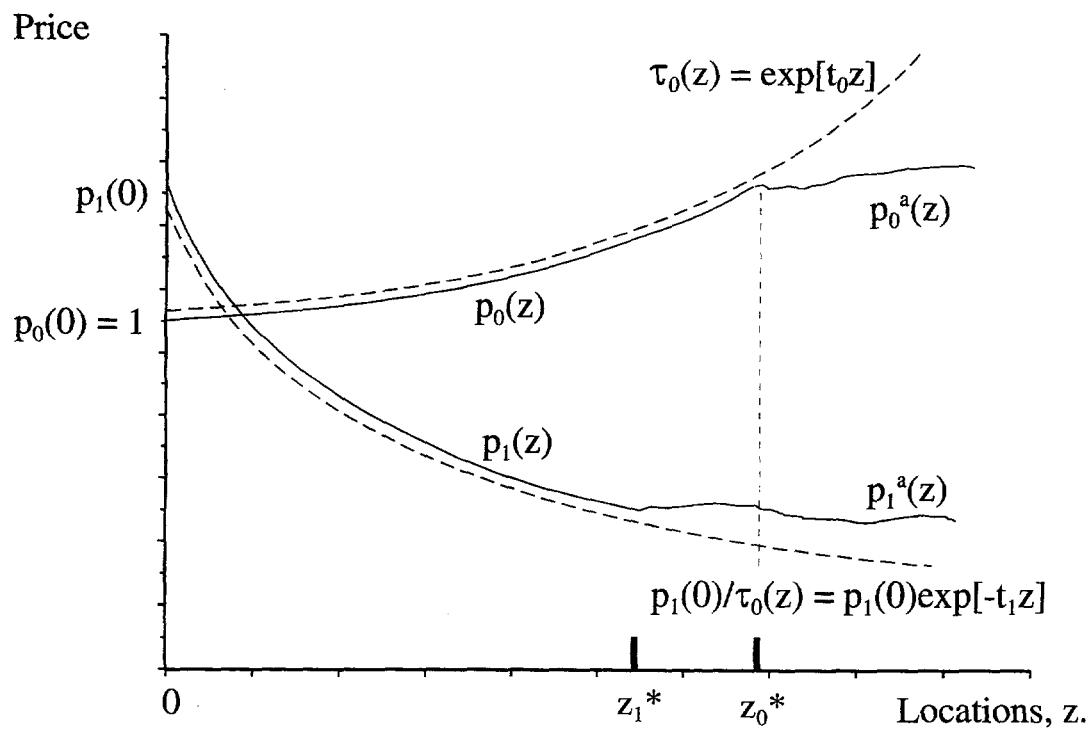


Figure 1: Transport costs and prices

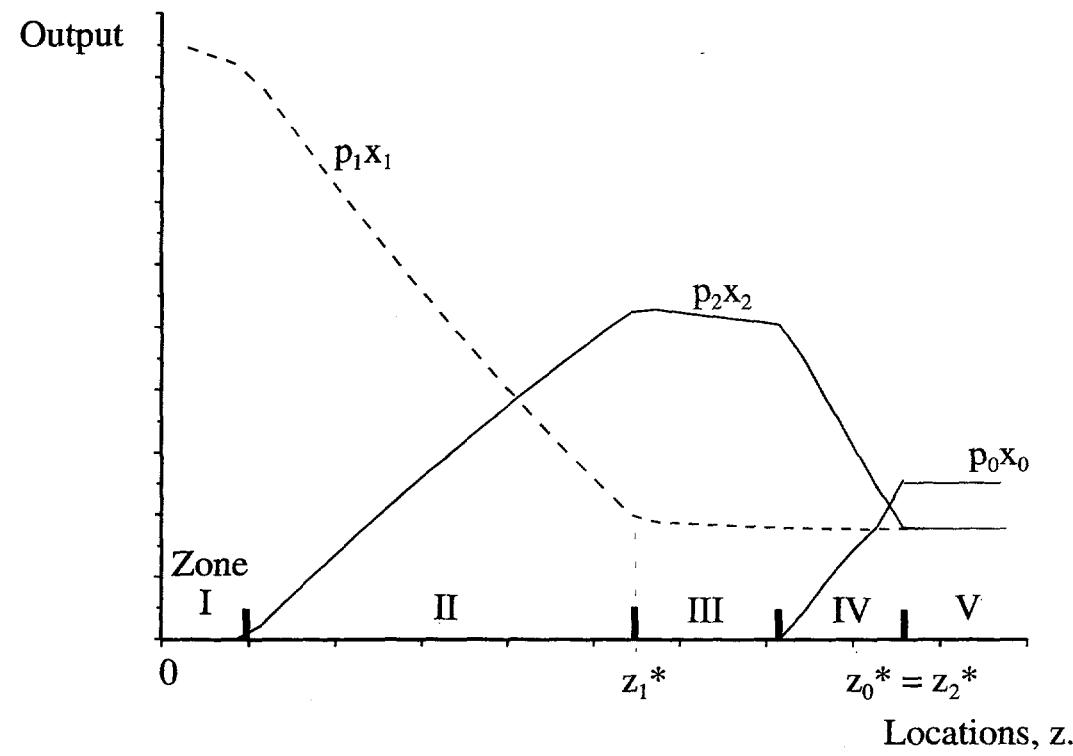


Figure 2: Zones of specialization

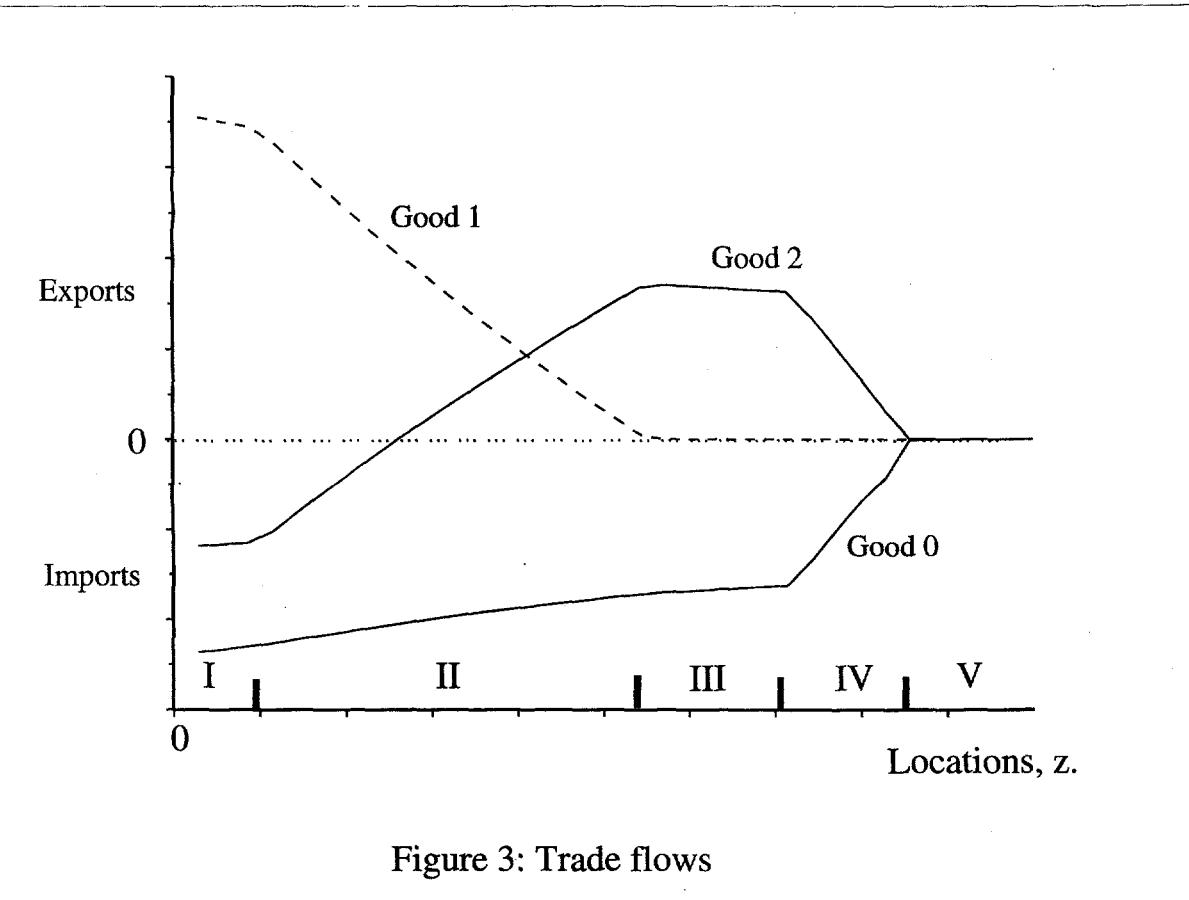


Figure 3: Trade flows

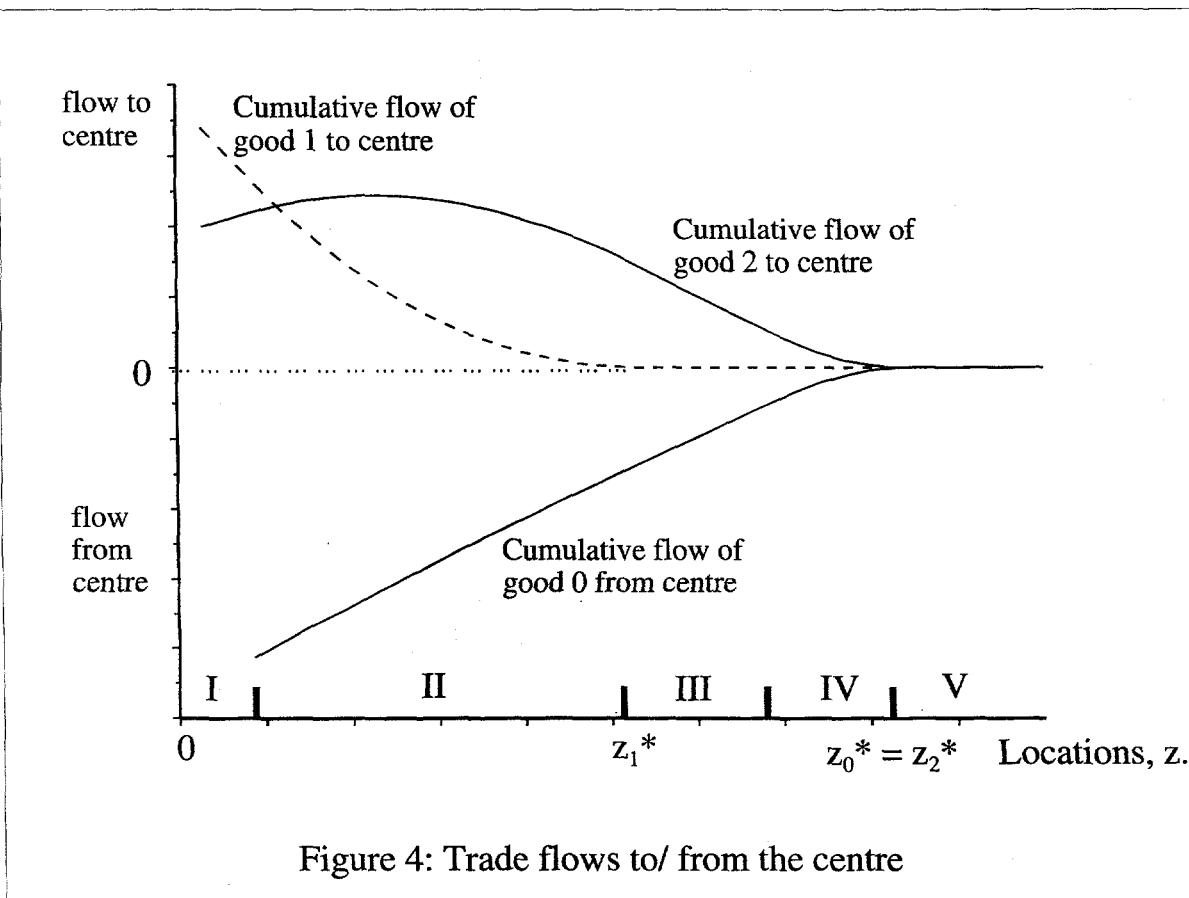


Figure 4: Trade flows to/ from the centre

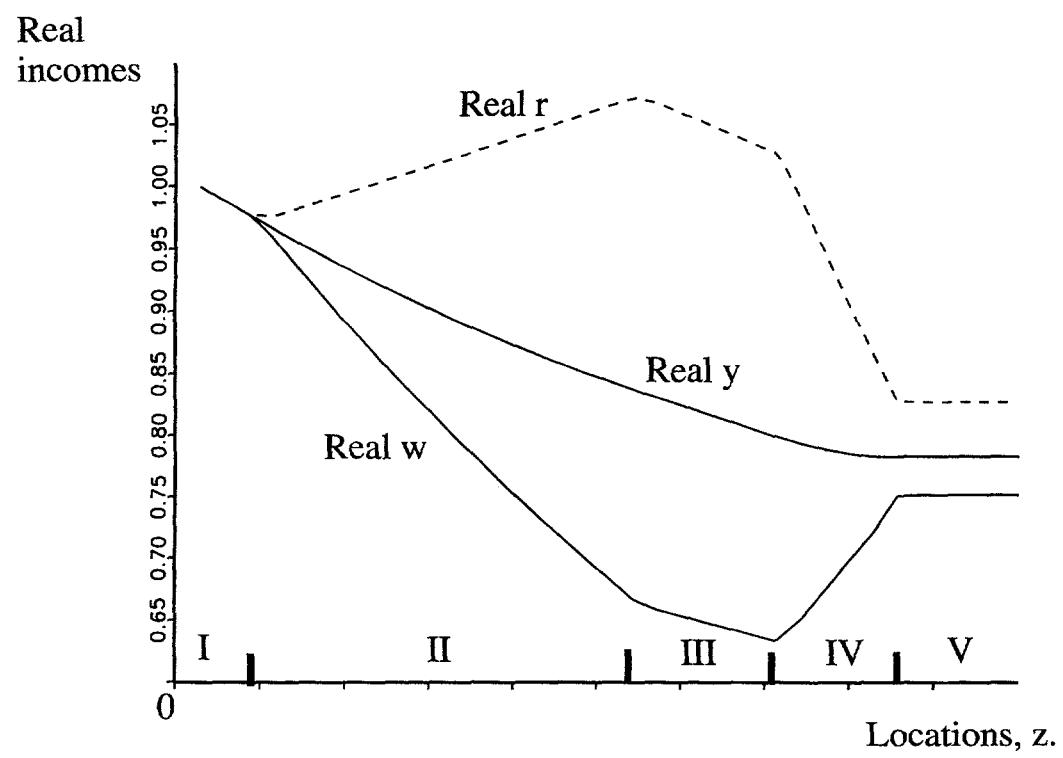


Figure 5: Factor prices and incomes

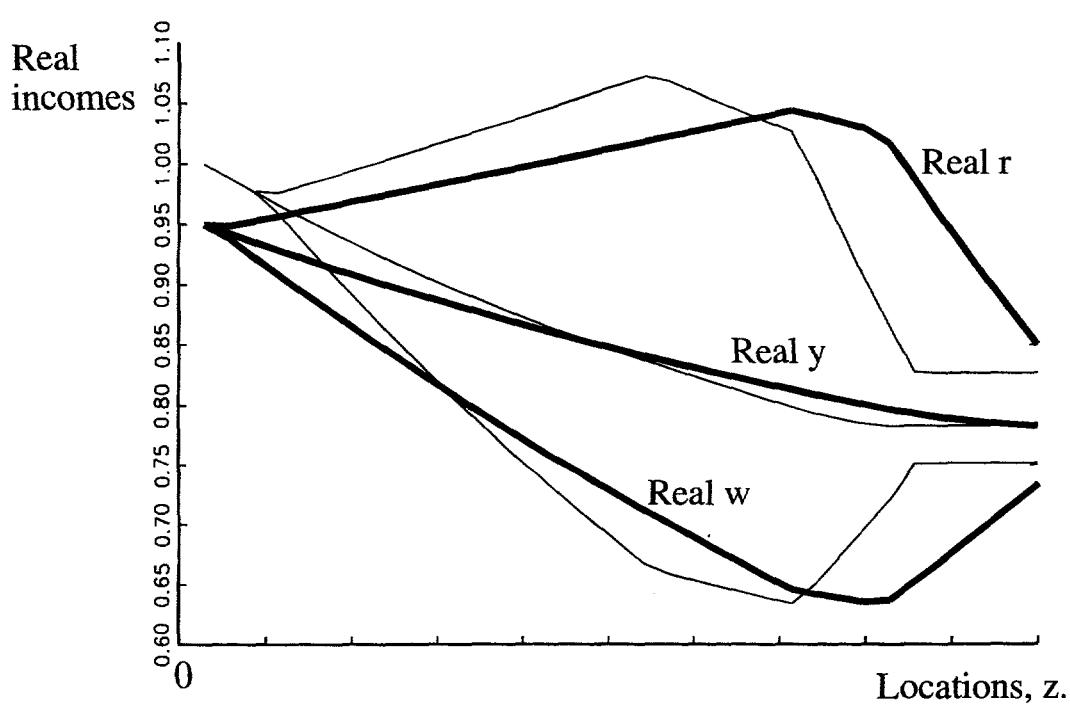


Figure 6: Lower transport costs and real income:  
initial (light) and final (bold) levels.

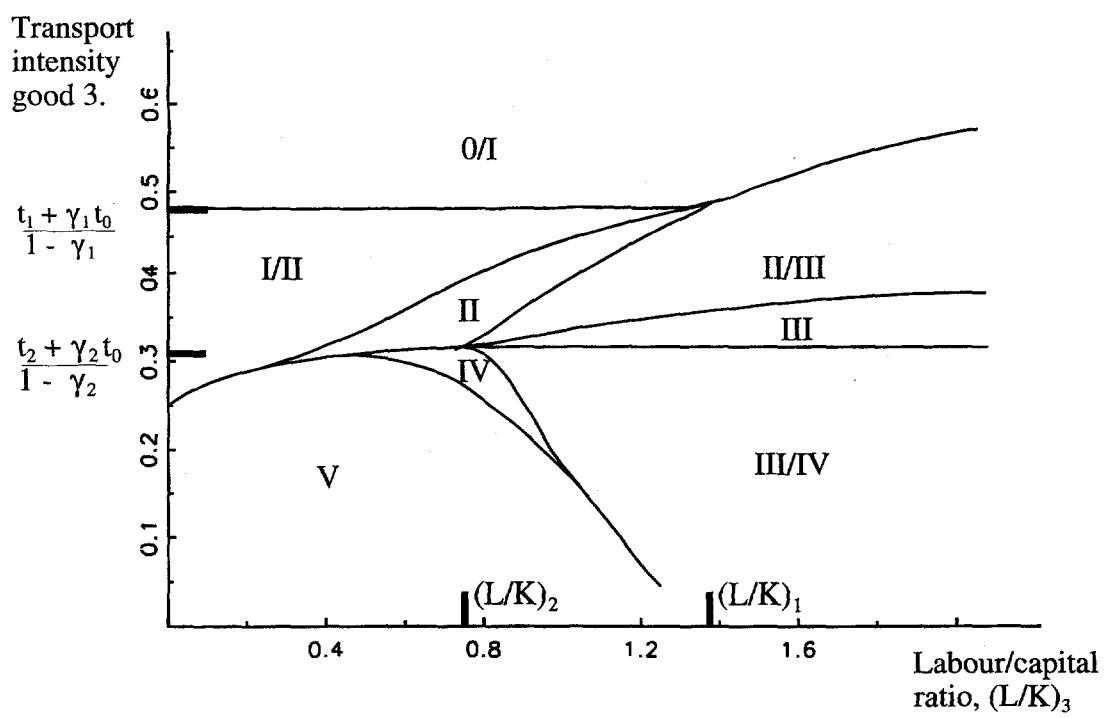


Figure 7: Location of a new activity



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